

# Curry

## A Tutorial Introduction

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# Preface

This book is about programming in **Curry**, a general-purpose declarative programming language that integrates functional with logic programming. Curry seamlessly combines the key features of functional programming (nested expressions, lazy evaluation, higher-order functions), logic programming (logical variables, partial data structures, built-in search), and concurrent programming (concurrent evaluation of constraints with synchronization on logical variables).

This book is best used as an introduction to Curry. Curry is a rigorously defined programming language. The **“Report”** is a still evolving, but fairly stable, document that precisely defines the language, in particular both its syntax and operational semantics. However, the report is not best suited to the beginner, rather it may be consulted in conjunction with this tutorial for the sake of a completeness that is not sought here.

There are several **implementations of Curry**. The examples and exercises in this book have been developed and executed using **PAKCS**. PAKCS is also accessible (in a restricted form) on-line via a **web-based system**. In this document, you find for many programs a **“Browse”** link which directly loads the program into this web-based system so that you can run or modify it. Alternatively, you can download the example programs and execute them on your locally installed Curry system.

## Part I

# Language Features

# Chapter 1

## Introduction

Curry is a universal programming language aiming at the amalgamation of the most important declarative programming paradigms, namely functional programming and logic programming. Curry combines in a seamless way features from functional programming (nested expressions, lazy evaluation, higher-order functions), logic programming (logical variables, partial data structures, built-in search), and concurrent programming (concurrent evaluation of constraints with synchronization on logical variables). Moreover, Curry provides additional features in comparison to the pure languages (compared to functional programming: search, computing with partial information; compared to logic programming: more efficient evaluation due to the deterministic evaluation of functions). Moreover, it also amalgamates the most important operational principles developed in the area of integrated functional logic languages: “residuation” and “narrowing” (see [12, 18] for surveys on functional logic programming).

The development of Curry is an international initiative intended to provide a common platform for the research, teaching<sup>1</sup> and application of integrated functional logic languages.

This document is intended to provide a tutorial introduction into the features of Curry and their use in application programming. It is not a formal definition of Curry which can be found in [21].

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<sup>1</sup>Actually, Curry has been successfully applied to teach functional and logic programming techniques in a single course without switching between different programming languages. More details about this aspect can be found in [13].

## Chapter 2

# Getting Started with Curry

There are different implementations of **Curry** available<sup>1</sup>. As such we can not describe the use of a Curry system in general. Some implementations are batch-oriented. In this case a Curry program is compiled into machine code and then executed. In this introduction we prefer an implementation that supports an interactive environment which provides faster program development by loading and testing programs within the integrated environment.

**PAKCS** (Portland Aachen Kiel Curry System) [4, 20]<sup>2</sup> contains such an interactive environment so that we show the use of this system here in order to get started with Curry. When you start the interactive environment of PAKCS (e.g., by typing “**pakcs**” as a shell command), you see something like the following output after the system’s initialization:

```
--      -
|_ \  | |           PAKCS - the Portland Aachen Kiel Curry System
  \ \ | |____
   / \ | ____|      Version 3.8.0 of 2025-04-07 (swi 9.0)
  / /\ \ |
 /_/ \_\ |          (using Curry Package Manager, version 3.3.0)

Type ":h" for help (contact: pakcs@curry-lang.org)
Prelude>
```

Now the system is ready and waits for some input. By typing “:q” (quit) you can always leave the system, but this is not what we intend to do now. The prefix of the current input line always shows the currently loaded module or program. In this case the module **Prelude** is loaded during system startup. The standard system module **Prelude** contains the definition of several predefined functions and data structures which are available in all Curry programs. For instance, the standard arithmetic functions like **+**, **\*** etc are predefined so that we can use the system as a simple calculator (the input typed by the user is underlined):

```
Prelude> 3+5*4
23
```

In this simple example you can already see the basic functionality of the environment: if

---

<sup>1</sup>Check the web page <https://www.curry-lang.org> for details.

<sup>2</sup><https://www.curry-lang.org/pakcs>

you type an expression, the system evaluates this expression to a *value* (i.e., an expression without evaluable functions) and prints this value as the result. Now you can type additional expressions to be evaluated. For instance, you can compare the values of two expressions with the usual comparison operators `>`, `<`, `<=`, `>=`:

```
Prelude> 3+5*4 >= 3*(4+2)
True
```

`==` and `/=` are the operators for equality and disequality and can be used on numbers as well as on other datatypes:

```
Prelude> 4+3 == 8
False
```

One may want to use Curry as more than a mere desk calculator. Therefore, we will discuss how to write programs in Curry. In general, a Curry *program* is a set of function definitions. The simplest sort of functions are those that do not depend on any input value, i.e., constant functions. For instance, a definition like

```
nine = 3*3
```

(such definitions are also called *rules* or *defining equations*) defines the name `nine` as equal to the value of `3*3`, i.e., `9`. This means that each occurrence of the name `nine` in an expression is replaced by the value `9`, i.e., the value of the expression `“4*nine”` is `36`.

Of course, it is more interesting to define functions depending on some input arguments. For instance, a function to compute the square value of a given number can be defined by

```
square x = x*x
```

Now it is time to make some remarks about the syntax of Curry (which is actually very similar to Haskell [22]). The names of functions and parameters usually start with a lowercase letter followed by letters, digits and underscores. The application of a function *f* to an expression *e* is denoted by juxtaposition, i.e., by *“f e”*. An exception are the *infix operators* like `+` or `*` that can be written between their arguments to enable the standard mathematical notation for arithmetic expressions. Furthermore, these operators are defined with the usual associativity and precedence rules so that an expression like `“2+3+4*5”` is interpreted as `((2+3)+(4*5))`. However, one can also enclose expressions in parenthesis to enforce the intended grouping.

If we write the definitions of `nine` and `square` with a standard text editor into a file (note that each definition must be written on a separate line starting in the first column) named `“firstprog.curry”` ([\[Browse Program\]](#)[\[Download Program\]](#)), we can load (and compile) the program into our environment by the command

```
Prelude> :l firstprog
```

which reads and compiles the file `“firstprog.curry”` and makes all definitions in this program visible in the environment. After the successful processing of this program, the environment shows the prefix to the input line as

```
firstprog>
```

indicating that the program “`firstprog`” is currently loaded. Now we can use the definitions in this program in the expressions to be evaluated:

```
firstprog> square nine
81
```

If we change our currently loaded program, we can easily reload the new version by typing “`:r`”. For instance, if we add the definition “`two = 2`” to our file “`firstprog.curry`”, we can reload the program as follows:

```
firstprog> :r
...
firstprog> square (square two)
16
```

Functions containing only a single arithmetic expression in the right-hand side of their defining equations might be useful abstractions of complex expressions but are generally only of limited use. More interesting functions can be written using conditional expressions. A *conditional expression* has the general form “`if c then e1 else e2`” where  $c$  is a Boolean expression (yielding the value `True` or `False`). A conditional expression is evaluated by evaluating the condition  $c$  first. If its value is `True`, the value of the conditional is the value of  $e_1$ , otherwise it is the value of  $e_2$ . For instance, the following rule defines a function to compute the absolute value of a number:

```
absolute x = if x>=0 then x else -x
```

Using recursive definitions, i.e., rules where the defined function occurs in a recursive call in the right-hand side, we can define functions whose evaluation requires a non-constant number of evaluation steps. For instance, the following rule defines the factorial of a natural number [[Browse Program](#)][[Download Program](#)]:

```
fac n = if n==0 then 1
        else n * fac(n-1)
```

Note that function definitions can be put in several lines provided that the subsequent lines start in a column greater than the column where the left-hand side starts (this is also called the *layout* or *off-side* rule for separating definitions).

You might have noticed that functions are defined by rules like in mathematics without providing any type declarations. This does not mean that Curry is an untyped language. On the contrary, Curry is a *strongly typed language* which means that each entity in a program (e.g., functions, parameters) has a type and ill-typed combinations are detected by the compiler. For instance, expressions like “`3*True`” or “`fac False`” are rejected by the compiler. Although type annotations need not be written by the programmer, they are automatically inferred by the compiler using a *type inference algorithm*. Nevertheless, it is a good idea to write down the types of functions in order to provide at least a minimal documentation of the intended use of functions. For instance, the function `fac` maps integers into integers and so its type can be specified by

```
fac :: Int -> Int
```

(`Int` denotes the predefined type of integers; similarly `Bool` denotes the type of Boolean values). If one is interested in the type of a function or expression inferred by the type inference algorithm, one can show it using the command “`:t`” in PAKCS:

```
absfac> :t fac
fac :: Int -> Int
absfac> :t fac 3
fac 3 :: Int
```

A useful feature of Curry (as well as most functional and logic programming languages) is the ability to define functions in a *pattern-oriented style*. This means that we can put values like `True` or `False` in arguments of the left-hand side of a rule and define a function by using several rules. The rule that matches the pattern of left-hand side will be called. For instance, instead of defining the negation on Boolean values by the single rule

```
not x = if x==True then False
        else True
```

we can define it by using two rules, each with a different pattern (here we also add the type declaration):

```
not :: Bool -> Bool
not False = True
not True  = False
```

The pattern-oriented notation becomes very useful in combination with more complex data structures, as we will see later.

One of the distinguishing features of Curry in comparison to functional languages is its ability to *search for solutions*, i.e., to compute values for the arguments of functions so that the functions can be evaluated. For instance, consider the following definitions of some functions on Boolean values contained in the prelude (note that Curry also allows functions defined as infix operators, i.e., “`x && y`” denotes the application of function `&&` to the arguments `x` and `y`):

```
False && _ = False
True  && x = x

False || x = x
True  || _ = True

not False = True
not True  = False
```

The underscore “`_`” occurring in the rules for `&&` and `||` denotes an arbitrary value, i.e., such an *anonymous variable* is used for argument variables that occur only once in a rule.

We can use these definitions to compute the value of a Boolean expression:

```
Prelude> True && (True || (not True))
```

True

However, we can do more and use the same functions to compute Boolean values for some (initially unknown) arguments:

```
Prelude> x && (y || (not x)) where x,y free  
{x=True, y=True} True  
{x=True, y=False} False  
{x=False, y=y} False
```

Note that the initial expression contains the *free variables* `x` and `y` as arguments. To support the detection of typos, free variables in initial expressions must be explicitly declared by a “`where...free`” clause at the end of the expression. Free variables denote “unknown” values. They are instantiated (i.e., replaced by some concrete values) so that the instantiated expression is evaluable. As we have seen above, replacing both `x` and `y` by `True` makes the expression reducible to `True`. Therefore, the Curry system shows in the first result line `True` together with the bindings (i.e., instantiations) of the free variables it has done to compute this value.

In general, there is more than one possibility to instantiate the arguments, e.g., the Boolean variables `x` and `y` can be instantiated to `True` or `False`. This leads to different solutions which are printed one after the other as shown above: there is one instantiation for `x` and `y` so that the instantiated expression evaluates to `True`, and there are two instantiations so that the instantiated expression evaluates to `False`. The last result line shows that the initial expression has the value `False` provided that `x` is instantiated to `False` but `y` can be arbitrary (i.e., `y` is not instantiated).

As we have seen, PAKCS evaluates and shows all the values (also called solutions if variables are instantiated) of an initial expression. This default mode can be changed by the command “`:set +interactive`”. In the *interactive mode*, we are asked after each computed value how to proceed: whether we want to see the next value (“yes”), no more values (“no”), or all values without any further interaction (“all”). Thus, we can show the values of the initial expression step-by-step as follows (note that it is sufficient to type the first letter of the answer followed by the “enter” key):

```
Prelude> :set +interactive  
Prelude> x && (y || (not x)) where x,y free  
{x=True, y=True} True  
More values? [Y(es)/n(o)/a(ll)] y  
{x=True, y=False} False  
More values? [Y(es)/n(o)/a(ll)] y  
{x=False, y=y} False  
More values? [Y(es)/n(o)/a(ll)] y  
No more values.
```

The final line indicates that there are no more values to the initial expression. This situation can also occur if functions are partially defined, i.e., there is a call to which no rule is applicable. For instance, assume that we define the function `pneg` by the single rule [\[Browse Program\]](#)[\[Download Program\]](#)

```
pneg True = False
```

then there is no rule to evaluate the call “pneg False”:

```
bool> pneg False  
*** No value found!
```

As we have seen in the Boolean example above, Curry can evaluate expressions containing free variables by guessing values for the free variables so that the expression becomes evaluable (the concrete strategy used by Curry will be explained later, but don’t worry: Curry is based on an optimal evaluation strategy [3] that performs these instantiations in a goal-oriented manner). However, we might not be interested to see all possible evaluations but only those that lead to a required result. For instance, we might be only interested to compute instantiations in a Boolean formula so that the formula becomes true, e.g., as in solving an equation.

For this purpose, Curry offers *constraints*, i.e., formulas that are intended to be solved (instead of computing an overall value). One of the basic constraints supported by Curry is equality, i.e., “ $e_1 ::= e_2$ ” denotes an *equational constraint* which is solvable whenever the expressions  $e_1$  and  $e_2$  (which must be of the same type) can be instantiated so that they are evaluable to the same value. For instance, the constraint “ $1+4 ::= 5$ ” is solvable, and the constraint “ $2+3 ::= x$ ” is solvable if the variable  $x$  is instantiated to 5. Now we can compute positive solutions to a Boolean expression by solving a constraint containing `True` on one side:

```
Prelude> (x && (y || (not x))) ::= True where x,y free  
{x=True, y=True} True
```

Curry allows the definition of functions by several rules and is able to search for several solutions. We can combine both features to define operations that yield more than one result for a given input. Such operations are called *non-deterministic operations*. A simple example for a non-deterministic operation is the following function `choose` which yields non-deterministically one of its arguments as a result [[Browse Program](#)][[Download Program](#)]:

```
choose x y = x  
choose x y = y
```

With this function we could have several results for a particular call:

```
choose> choose 1 3  
1  
3
```

We can use `choose` to define other non-deterministic operations:

```
one23 = choose 1 (choose 2 3)
```

Thus, a call to `one23` delivers one of the results 1, 2, or 3. Such a function might be useful to specify the domain of values for which we want to solve a constraint. For instance, to search for values  $x \in \{1, 2, 3\}$  satisfying the equation  $x + x = x * x$ , we can solve this constraint

( $c_1 \& c_2$  denotes the conjunction of the two constraints  $c_1$  and  $c_2$ ):

```
choose> x:=one23 & x+x:=x*x where x free  
{x=2} True
```

The advantages of non-deterministic operations will become clear when we have discussed the (demand-driven) evaluation strategy in more detail.

This chapter is intended to provide a broad overview of the main features of Curry and the use of an interactive programming environment so that one can easily try the subsequent examples. In the next chapter, we will discuss the features of Curry in more detail.

## Chapter 3

# Main Features of Curry

### 3.1 Overview

The major elements declared in program are *functions* and *data structures*.

- A *function* or *operation* defines a computation similar to an expression. However, the expression computed by a function has a name and is often parameterized. These characteristics enable you to execute the same computation, possibly with different parameters, over and over in the same program by simply invoking the computation's name and setting the values of its parameters. A function also provides a *procedural abstraction*. Rather than coding a computation by means of a possibly complicated expression, you can factor out portions of this computation and abstract them by their names.
- A *data structure* is a way to organize data. For example, you can record the movements of your bank account in a column in which deposits are positive numbers and withdrawals are negative numbers. Or you can record the same movements in two columns, one for deposits and another for withdrawals, in which all numbers are positive. With the second option, the columns rather than the signs specialize the meaning of the numbers. The way in which information is organized may ease some computations, such as retrieving portions of information, and is intimately related, through pattern matching, to the way in which functions are coded.

This section describes in some detail both of these features and a number of related concepts. Curry has some additional features not described in this section. Since they are useful to support particular programming tasks, we introduce them later when we discuss such programming techniques.

### 3.2 Expressions

A function can be regarded as a parameterized expression with a name. Thus, we begin by explaining what an expression is and how it is used. Most expressions are built from simpler subexpressions, a situation that calls for a recursive, or inductive, definition.

An *expression* is either a symbol or literal value or is the application of an expression to another expression.

A symbol or literal value is referred to as an *atom*. For example, numbers and the Boolean symbols “True” and “False” are examples of atoms. Atoms constitute the most elementary expressions. These elementary expressions can be combined to create more complex expressions, e.g., “2 + 3” or “not True”. The combination is referred to as a *function application*. Since a function application is a very common activity, it is convenient to denote it as simply as possible. This convenience is obtained to the extreme by writing the two expressions one near the other as in “not True”. This notation is referred to as *juxtaposition*.

In the above expressions, the symbols “+” and “not” are operations. Both are predefined in the standard library `Prelude`. Although conceptually the symbols “+” and “not” are alike, syntactically they differ. The symbol “+” is a *infix operator* as in the ordinary mathematical notation. Infix operators have a *precedence* and an *associativity* so that the expression “2 + 3 \* 4” is understood as “2 + (3 \* 4)” and the expression “4 - 3 - 2” is understood as “(4 - 3) - 2”. The precedence and associativity of an infix symbol are defined in a program by a declaration. The following declarations, from the prelude, define these parameters for some ordinary arithmetic operations:

```
infixl 7 *, 'div', 'mod'
infixl 6 +, -
infix 4 <, >, <=, >=
```

For example, the precedence of the addition and subtraction operators is 6 and their associativity is left. The relational operators have precedence 4 and are not associative. Operators with a higher precedence bind stronger, i.e., the expression “4 < 2 + 3” is interpreted as “4 < (2 + 3)”.

*Infix declarations* must always occur at the beginning of a program. The precedence of an operator is an integer between 0 and 9 inclusive. The associativity of an operator is either *left*, denoted by the keyword “infixl” or *right*, denoted by the keyword “infixr”. Non-associative infix operators are declared using the keyword “infix”.

Most often, an infix operator is any user-defined sequence of characters taken from the set “~!@#%&\*+ -= <>?./|\:”. Alphanumeric identifiers can be defined and used as infix operators if they are surrounded by backquotes, as “`div`” and “`mod`” in the previous declaration. For example, for any integer value  $x$ , the following expression evaluates to  $x$  itself.

```
x `div` 2 * 2 + x `mod` 2
```

Non-infix symbols are *prefix*. They are applied by prefixing them to their arguments as in “not True”.

**Exercise 1** Define a predicate, read as “factors” and denoted by the infix operator “./.”, that tells whether an integer is a factor of another integer. The predicate should work for every input and 0 should not be a factor of any integer. The operator should be non-associative and have precedence 7. [[Browse Answer](#)][[Download Answer](#)]

A symbol, whether infix or prefix, can only be applied to values of an appropriate type. As one would expect, the Boolean negation operator can be applied only to a Boolean value. For example, the expression “not 2” is an error. The compiler/interpreter would report that the expression is incorrectly typed. We will discuss types in more detail after presenting data declarations.

The application of an expression to another is a binary operation. The expression that is being applied is referred to as the *function* of the application. The other expression is referred to as the *argument*. Thus, in “not True”, “not” is the function and “True” is the argument. The situation is slightly more complicated for infix operations. The reading of “2+3” is that the function “+” is applied to the expression “2”. The result is a function which is further applied to the expression “3”.

Expressions can also be conditional, i.e., depend on the value of a Boolean expression. Such *conditional expressions* have the form “if  $b$  then  $e_1$  else  $e_2$ ”. The value of this expression is the value of  $e_1$  if  $b$  evaluates to `True`, or the value of  $e_2$  if  $b$  evaluates to `False`. Thus, the value of “if 3>4 then 2\*2 else 3\*4” is 12.

### 3.3 Predefined Types

A *type* is a set of values. Ubiquitous types, such as integers or characters, are predefined by most programming languages. Curry makes no exception. These types are referred to as *builtin* and are denoted with a familiar, somewhat special, syntax. Both the availability of builtin types and their characteristics may depend on a specific implementation of Curry. The following table summarizes some types available in **PAKCS**.

Type	Declaration	Examples
Integer	<code>Int</code>	<code>...</code> , -2, -1, 0, 1, 2, <code>...</code>
Boolean	<code>Bool</code>	<code>False</code> , <code>True</code>
Character	<code>Char</code>	<code>'a'</code> , <code>'b'</code> , <code>'c'</code> , <code>...</code> , <code>'\n'</code> , <code>...</code>
String	<code>String</code>	<code>"hello"</code> , <code>"world"</code>
List of $\tau$	<code>[<math>\tau</math>]</code>	<code>[]</code> , <code>[0,1,2]</code> , <code>0:1:2:[]</code>
Unit	<code>()</code>	<code>()</code>

The details of these types are found in the **PAKCS** User Manual. Below, we only outline a few crucial characteristics of the builtin types. The integers have arbitrary precision. Some frequently used non-printable characters are denoted, as in other popular programming languages, by escape sequences, e.g., *newline* is denoted by `\n`. The type *List* represents sequences of values. This type is polymorphic, i.e., for any type  $\tau$ , the type list of  $\tau$ , denoted by “`[ $\tau$ ]`”, is a type whose instances are sequences of instances of  $\tau$ . The last two examples in the *List* row of the table denote a list of integers, their type denoted by “`[Int]`”. The notation of lists will be further discussed later. The symbol “`()`” denotes the unit type as well as the only element of this type. The unit type is useful in situations where the return value of a function is not important. Another useful type available in **PAKCS**, the *tuple*, will be described later.

### 3.4 Predefined Operations

Many frequently-used functions and infix operators, similar to frequently-used types, are predefined in Curry. Some of these can be found in the “Prelude”, a Curry source program automatically loaded when the compiler/interpreter starts. A few others are so fundamental that they are built into the language. Some of these functions and operators are shown in the following table.

Description	Ident.	Fix.	Prec.	Type
Boolean equality	<code>==</code>		4	<code>a -&gt; a -&gt; Bool</code>
Constrained equality	<code>:=:</code>		4	<code>a -&gt; a -&gt; Bool</code>
Boolean conjunction	<code>&amp;&amp;</code>	R	3	<code>Bool -&gt; Bool -&gt; Bool</code>
Boolean disjunction	<code>  </code>	R	2	<code>Bool -&gt; Bool -&gt; Bool</code>
Parallel conjunction	<code>&amp;</code>	R	0	<code>Bool -&gt; Bool -&gt; Bool</code>
Constrained expression	<code>&amp;&gt;</code>	R	0	<code>Bool -&gt; a -&gt; a</code>

Because of non-determinism and free variables, in the following discussion, different evaluations of the same expression may produce different values.

The *Boolean equality* applied to expressions  $u$  and  $v$ , i.e.,  $u == v$ , returns “True” when  $u$  and  $v$  evaluate to the same *value* and “False” when they evaluate to different *values*—a more precise definition will be given later. If the evaluation of  $u$  and/or  $v$  ends in an expression that still contains functions, e.g., `1 ‘div’ 0`, the computation *fails* and no value is returned.

The *constrained equality* applied to expressions  $u$  and  $v$ , i.e.,  $u :=: v$  returns “True” when  $u$  and  $v$  evaluate to the same *value*—a precise definition will be given later. Otherwise, the computation *fails* and no value is returned. A key difference between the Boolean and the constrained equalities is how they evaluate expressions containing variables. This will be discussed in some detail in Section 3.14.1.

The *Boolean conjunction* applied to expressions  $u$  and  $v$ , i.e.,  $u \&\& v$ , returns “True” when  $u$  and  $v$  evaluate to “True”.

The *Boolean disjunction* applied to expressions  $u$  and  $v$ , i.e.,  $u || v$ , returns “True” when  $u$  or  $v$  evaluate to “True”.

The *parallel conjunction* applied to expressions  $u$  and  $v$ , i.e.,  $u \& v$ , evaluates  $u$  and  $v$  concurrently. If both succeeds, the evaluation succeeds; otherwise it fails.

The *constrained expression* applied to a constraint  $c$  and an expression  $e$ , i.e.,  $c \&> e$ , evaluates first  $c$  and, if  $c$  evaluates to “True”, then the result is the value of  $e$ , otherwise it fails.

Curry predefines many more functions and operations, e.g., the standard arithmetic and relational operators on numbers. A complete list can be found both in the Report and the “Prelude”.

## 3.5 Functions

### 3.5.1 Basic Concepts

A program function abstracts a function in the mathematical sense. A function is a device that takes arguments and returns a result. The result is obtained by evaluating an expression which generally involves the function's arguments. The following function computes the *square* of a number.

```
square x = x * x
```

The symbols “`square`” is the name or *identifier* of the function. The symbol “`x`” is the function's *argument*. The above declaration is referred to as a *rewrite rule*, or simply a rule, defining a function. The portion of the declaration to the left of the symbol “`=`” is the rule's *left-hand side*. The expression “`x * x`” is the rule's *right-hand side*.

When the “`square`” symbol is applied to an expression, e.g., “`2 + 3`”, this expression is *bound* to the argument “`x`”. The result of the application is “`(2 + 3) * (2 + 3)`”, i.e., the body in which the argument is replaced by its binding. Thus:

```
Prelude> square (2+3)
25
```

Functions can be *anonymous*, i.e., without a name. An anonymous function is useful when a function is referenced only once. In this case, the reference to the function can be replaced by the expression defining the function. In the following example:

```
result = (\x -> x * x) (2+3)
```

the value of `result` is 25. It is obtained by applying the expression `(\x -> x * x)`, an anonymous function, to `(2+3)`, its argument. An anonymous function definition has the following structure:

```
\ <arguments> -> <right-hand side>
```

The arguments are listed as in any rewrite rule. The right-hand side is the expression to be evaluated when the anonymous function is applied to actual arguments. A more motivating example of anonymous function is presented in Section 3.11

The evaluation of any expression, in particular of a function application, is *lazy*. This means that the computation of any expression, including the subexpressions of a larger expression, is delayed until the expression's value is actually needed. The exact meaning of “actually needed” is quite technical, but the intuitive meaning suffices for our purposes. Many programming languages, such as C and Java, adopt this evaluation strategy, under the name of *short circuit*, only for Boolean expressions.

We will discuss this issue in more detail later. Although the lazy evaluation strategy is conceptually simpler than any other strategy, many traditional programming languages evaluate the arguments of a function call eagerly, i.e., before applying a function to its arguments. This fact is sometimes a source of confusion for the beginner.

### 3.5.2 Pattern Matching

The definition of a function can be broken into several rules. A single rule would suffice in many cases. However, several rules allows a definition style, called *pattern matching*, which is easier to code and understand. This feature allows a function to dispatch the expression to be returned depending on the values of its arguments. The following example shows the definition of the Boolean negation function “not”:

```
not True = False
not False = True
```

The above definition is equivalent to the following one which does not use pattern matching but relies on a conditional expression:

```
not x = if x == True then False else True
```

Pattern matching is particularly convenient for functions that operate on algebraic datatypes. We will further discuss this aspect after discussing data declarations.

### 3.5.3 Conditions

Each rule defining a function can include one or more *conditions*. For Boolean conditions, a rule has the following general structure:

$$\begin{array}{l} \text{functId } arg_1 \dots arg_m \mid \text{cond}_1 = \text{expr}_1 \\ \mid \dots = \dots \\ \mid \text{cond}_n = \text{expr}_n \end{array}$$

A condition is tested after binding the arguments of a call to the corresponding arguments in the left-hand side of the rule. The function is applied to the arguments only if the condition holds. Each condition  $\text{cond}_i$  is an expression of type `Bool`. The conditions are tested in their textual order. Thus, the first right-hand side with a condition evaluable to `True` is taken. Furthermore, the last condition can be “otherwise” which is equivalent to `True`, i.e., it holds regardless of any value of the arguments. The following example shows a plausible definition of the maximum of two numbers:

```
max x y | x < y      = y
        | otherwise = x
```

### 3.5.4 Non-determinism

Operations can be *non-deterministic*. Non-deterministic operations are not functions in the mathematical sense because they can return different values for the same input. For example, a hospital’s information system defines which days a doctor is on-call with a non-deterministic function:

```
oncall Joan      = Monday
oncall Joan      = Wednesday
oncall Richard = Monday
```

```
oncall Luc      = Tuesday
...
```

The value of “oncall Joan” can be either “Monday” or “Wednesday”. The programmer cannot select which of the two values will be computed. Non-deterministic operations support a programming style similar to that of logic programs, while preserving some advantages of functional programs such as expression nesting and lazy evaluation. In particular, some strong properties concerning the evaluation of ordinary functions hold also for non-deterministic operations [2]. For example, suppose that “today” holds which day of the week is today. A predicate, “available”, telling whether its argument, a doctor, is available at the current time is coded as:

```
available x | oncall x == today = True
           | otherwise          = False
```

Without non-determinism, coding “oncall” would require some data structure, e.g., the list of days in which each doctor is on-call, and defining “available” would become more complicated.

Non-determinism is a powerful feature. In programming, as in other aspects of life, power must be exercised with some care. A non-deterministic program is appropriate only if all its possible outputs are equally desirable. If some outputs are more desirable than others, the program should be (more) deterministic. In this case, non-determinism could be conveniently used internally by the program to generate plausible results which can then be selected according to desirability.

**Exercise 2** In a manufacturing plant two specialized tasks, `cut` and `polish`, are executed only by specialized workers, `Alex`, `Bert` and `Chuck`. Not every worker can execute every task. Only `Alex` and `Bert` are able to `Cut`, whereas only `Bert` and `Chuck` are able to `Polish`. Code a non-deterministic operation, `assign`, that assigns to a task a worker that can execute it. [\[Browse Answer\]](#)[\[Download Answer\]](#)

### 3.5.5 Functional Patterns

Pattern matching, see Sect. 3.5.2, is a feature that provides in a compact and readable form both case distinction and (sub)argument selection. The arguments in a rule defined by pattern matching are expressions consisting of variables and/or data constructor symbols. Curry amplifies this feature with functional patterns. In a *functional pattern* some argument in a rule defining a function is an expression containing a function symbol. For example, the function computing the last element of a non-empty list can be defined as:

```
last (_++[e]) = e
```

where “++” is an infix operator that concatenates two lists, see function `conc` in Sect. 3.7. The intuition is that if a list  $l$  can be seen as the concatenation of some uninteresting list and a list containing the single element  $e$ , then  $e$  is the last element of  $l$ .

The meaning of the above rule is the same as the infinite set of rules:

```

last [e] = e
last [_ , e] = e
last [_ , _ , e] = e
...

```

Code employing functional patterns should be preferred to similar code using conditions (see below) because it is more readable and more efficient:

```

last xs | xs == _++[e] = e where e free

```

**Exercise 3** Define a function that takes a list  $a$  of integers and computes a sublist  $l$  of  $a$  such that the last element of  $l$  is twice the first element. E.g., given the list  $[3, 6, 2, 1, 4, 5]$  the sublists satisfying the required constraint are  $[3, 6]$  and  $[2, 1, 4]$ . [\[Browse Answer\]](#)[\[Download Answer\]](#)

### 3.5.6 Default Rule

The Curry language specifies that the textual order of the rules defining a function is irrelevant in the sense that every rule that is applicable to an expression should be applied. In practice, the situation is more delicate. For example, in **PAKCS** when multiple rules are applicable some rule is going to be applied before some other and if the application of the first rule does not terminate the second rule is never applied.

When defining a function, Curry allows the programmer to define a rule, called a *default* rule [8] that is applied only if all the other rules, that in this context we call *standard*, cannot be applied. The processing of default rules require the Curry preprocessor. It is not part of **PAKCS** but the preprocessor can easily be installed by the Curry package manager with the following commands (see also Section 5.2):

```

> cypm update
> cypm install currypp

```

After the installation of the Curry preprocessor,<sup>1</sup> one can use default rules in a program by placing the following line at the beginning of the source program.

```

{-# OPTIONS_CYMAKE -F --pgmF=currypp --optF=defaultrules #-}

```

We recall that a standard rule  $r$  is applicable to an expression  $e$  iff  $e$  and the left-hand side of  $r$  unify and the condition of  $r$ , if any exists, is satisfied by the instantiation of  $e$ . For example, the operation `zip` is defined with a default rule as follows:

```

zip (x:xs) (y:ys) = (x,y) : zip xs ys
zip'default _ _ = []

```

Since the standard rule is applicable to `zip [1] [2]`, the default rule is ignored so that this expression is solely reduced to `(1,2):zip [] []`. Since the standard rule is not applicable to `zip [] []`, the default rule is applied and yields the value `[]`. Altogether, the only value of

---

<sup>1</sup>The executable `currypp` of the preprocessor is stored in `$HOME/.cpm/bin` so that one should have this directory in the load path.

`zip [1] [2]` is `[(1,2)]`. However, if some argument has more than one value, we use the evaluation principle above for each combination. Thus, the call `zip ([1] ? []) [2]` yields the two values `[(1,2)]` and `[]`.

Default rules are useful to regain control after a failed search. For example, consider looking up the value of a key in a key-value pair list.

```
lookup (key, _ ++ [(key,value)] ++ _) = Just value
lookup'default _ = Nothing
```

If the key of a search is not in a list  $l$ , the call `lookup l` returns `Nothing` instead of failing.

**Important note:** Default rules can only be added to operations defined at the top-level (i.e., not to locally defined operations, see Section 3.13). A reason for this restriction is that default rules are applied after searching for all possibilities to apply a previous standard rule. With local definitions, the precise scope of the “previous” search is difficult to define.

## 3.6 User-defined Types

A *type* is a set of values. Some common types, presented in Section 3.3, are built into the language and the programmer does not declare them. All other types used in a program must be declared by the programmer. The classification of some types as builtin vs. user-defined is only a matter of convenience. Builtin and user-defined types are conceptually very similar. In fact, the declaration of some builtin types could have been left to the programmer. For example:

```
data Boolean = False | True
```

is exactly how the builtin “Boolean” type would be declared if it were not builtin. In this declaration, the identifier “Boolean” is referred to as a *type constructor*, whereas the identifiers “False” and “True” are referred to as *data constructors*. The following declarations, very similar to the previous one, define plausible types “WeekDay” and “PrimaryColor”.

```
data WeekDay = Monday | Tuesday | Wednesday | Thursday | Friday
```

```
data PrimaryColor = Red | Green | Blue
```

All these types are finite, i.e., they define a finite set of values, and resemble enumerated types in the Pascal or C languages.

The declaration of an infinite type is similar, but as one should expect, must be (directly or indirectly) recursive. The following declaration defines a binary tree of integers. We recall that the typical definition of this type says that a *binary tree* is either a *leaf* or it is a *branch* consisting of two binary trees. Not surprisingly, this definition is recursive which accounts for an infinity of trees. The words “leaf” and “branch” are conventional names used to distinguish the two kinds of trees and have no other implicit meaning. Often, branches include a *decoration*, a value of some other arbitrary type. If a tree  $T$  is a branch, the two trees in the branch are referred to as the left and right children of  $T$ . A declaration defining binary trees where the decoration is an integer follows:

```
data IntTree = Leaf | Branch Int IntTree IntTree
```

All the following expressions are values of type “IntTree”:

```
Leaf
Branch 0 Leaf Leaf
Branch 7 (Branch 5 Leaf Leaf) (Branch 9 Leaf Leaf)
```

The first tree is a leaf and therefore it contains no decoration. The second tree contains a single decoration, “0”, and two children both of which are leaves. The third tree contains three decorations. Binary trees are interesting because many efficient searching and sorting algorithms are based on them.

User-defined types can be parameterized by means of other types similar to the builtin type list introduced in Section 3.3. These types are called *polymorphic*. For example, if the type of the decoration of a binary tree is made a parameter of the type of the tree, the result is a polymorphic binary tree. This is achieved by the following declaration [[Browse Program](#)][[Download Program](#)]:

```
data BinTree a = Leaf | Branch a (BinTree a) (BinTree a)
```

The identifier “a” is a *type variable*. Observe that the type variable not only defines the type of the decoration, but also the type of the subtrees occurring in a branch. In other words, the type that parameterizes a tree also parameterizes the children of a tree. The type variable can be implicitly or explicitly bound to some type, e.g., “Int” or “WeekDay” defined earlier. For example, a function that looks for the string “Curry” in a tree of strings is defined as [[Browse Program](#)][[Download Program](#)]:

```
findCurry Leaf          = False
findCurry (Branch x l r) = x == "Curry" || findCurry l || findCurry r
```

The type of the argument of function “findCurry” is “BinTree String”. The binding of type “String” to the type variable of the definition of the polymorphic type “BinTree” is automatically inferred from the definition of function “findCurry”.

A polymorphic type such as “BinTree” can be specialized by binding its variable to a specific type by an explicit declaration as follows [[Browse Program](#)][[Download Program](#)]:

```
type IntTree = BinTree Int
```

where “type” is a reserved word of the language. This declaration defines “IntTree” as a synonym of “BinTree Int”. The synonym can be used in *type declarations* to improve readability. The following example defines a function that tallies all the decorations of a tree of integers [[Browse Program](#)][[Download Program](#)]:

```
total :: IntTree -> Int
total Leaf          = 0
total (Branch x l r) = x + total l + total r
```

**Exercise 4** Pretend that list is not a builtin type, with special syntax, of the language. Define your own type list. Define two functions on this type, one to count how many elements

are in a list, the other to find whether some element is in a list. [\[Browse Answer\]](#)[\[Download Answer\]](#)

### 3.7 Lists

The type `list` is builtin or predefined by the language. This type could be easily defined by the programmer, see Exercise 4, except that the language allows the representation of lists in a special notation which is more agile than that that would be available to the programmer. The following statement defines important concepts of a list:

A *list* is either *nil* or it is a *cons* consisting of an element, referred to as the *head* of the list, and another list, referred to as the *tail* of the list.

The `nil` list is denoted by “`[]`”, which is read “`nil`”. A `cons` list, with head  $h$  and tail  $t$  is denoted by “ $h:t$ ”. The infix operator “`:`”, which is read “`cons`”, is right associative with precedence 5. A list can also be denoted by enumerating its elements, e.g., “`[u,v,w]`” is a list containing three elements, “`u`”, “`v`” and “`w`”, i.e., it is just another notation for “`u:v:w:[]`”. The number of elements is arbitrary. The elements are enclosed in brackets and separated by commas.

The following functions concatenate two lists and reverse a list, respectively. The “`Prelude`” defines the first one as the infix operator “`++`” and the second one, much more efficiently, as the operation “`reverse`”.

```
conc []      ys = ys
conc (x:xs) ys = x : conc xs ys

rev []      = []
rev (x:xs) = conc (rev xs) [x]
```

Several *ad hoc* notations available for lists are described in Sections 4.2.3 and 4.2.4.

A key advantage of these special notations for lists is a reduction of the number of parentheses needed to represent list expressions in a program. This claim can be easily verified by comparing the builtin notation with the ordinary notation which was the subject of Exercise 4.

### 3.8 Strings

Although “`String`” is a predefined type (see Section 3.3), there are no special operations on strings. The reason is that “`String`” is just another name for “`[Char]`”, i.e., strings are considered as lists of characters. In addition, Curry provides a handy notation for string constants, i.e., the string constant

```
"hello world"
```

is identical to the character list

```
['h','e','l','l','o',' ','w','o','r','l','d']
```

Thus, any operation applicable to arbitrary lists can also be applied to strings. For instance, the prelude defines an infix operator “++” to concatenate lists and the function “reverse” to reverse the order of all lists elements (similarly to `conc` and `rev` in Section 3.7). Thus, we can also use them to operate on strings:

```
Prelude> "Hi"++"Hi"
"HiHi"
Prelude> reverse "hello"
"olleh"
```

### 3.9 Tuple

The word “tuple” is a generic name for a family of related types. A tuple in a program is similar to a tuple in mathematics, i.e., a fixed length sequence of values of possibly different types. Examples of tuples are pairs and triples. They could be defined by the programmer as follows:

```
data Pair a b = Pair a b

data Triple a b c = Triple a b c
```

These types are polymorphic. Observe the two occurrences of the identifiers “Pair” and “Triple” in the above declarations. The occurrence to the left names a type constructor, whereas the occurrence to the right names a data constructor. These symbols are *overloaded*. However, this kind of overloading causes no problems since type expressions are clearly separated from value expressions. The type variables “a”, “b”... can be bound to different types.

For example, the information system of a “Big & Tall” shoe store declares a function that defines the largest size and width of each model [[Browse Program](#)][[Download Program](#)]:

```
data Width = C | D | E | EE | EEE | EEEE
largest "New Balance 495" = Pair 13 EEE
largest "Adidas Comfort" = Pair 15 EE
...
```

The language predefines tuples and denotes them with a special notation similar to the standard mathematical notation. Using predefined tuples, the above function is coded as:

```
largest "New Balance 495" = (13,EEE)
largest "Adidas Comfort" = (15,EE)
...
```

Tuples are denoted by a fixed-length sequence of comma-separated values between parentheses. There is no explicit data constructor identifier. The type of a tuple is represented as a tuple as well, e.g., the type of “largest” can be defined as:

```
largest :: String -> (Int,Width)
```

## 3.10 Type classes

A type class defines a generic interface abstracting some common feature over a variety of types. For example, many numeric structures, such as integer, vectors and matrices, allow the addition of elements in the structure. We capture the property of “being *addable*” as follows:

```
class Addable a where
  (+) :: a -> a -> a
```

The variable `a` is a type parameter. The identifier “+” is chosen because we are generalizing addition, but it is not the usual addition of integers. Any symbols would be acceptable:

To say that some structure is *addable* we use an *instance* declaration. For example, the following declaration states that the integers are addable and the addition operation is the addition function defined in the Prelude.

```
instance Addable Int where
  x + y = x Prelude.+ y
```

Next, we represent vectors (without an explicit data declaration) as lists of *addables* and we define the addition of vectors as the component-wise addition of their elements:

```
instance Addable a => Addable [a] where
  xs + ys = zipWith (+) xs ys
```

The symbol “+” refers to the same symbol defined in the `Addable` type class and it is applied to the vectors’ elements. With these definitions we can add two vectors as follows:

```
testv :: [Int]
testv = [1,2,3] + [4,5,6]
```

**Exercise 5** Define a matrix as follows:

```
data Matrix a = Matrix [[a]]
```

and make it *addable* using an instance declaration. [\[Browse Program\]](#)[\[Download Program\]](#)

## 3.11 Higher-Order Computations

The arguments of a function can be functions themselves. This feature is banned or restricted by many programming languages. E.g., in C only a *pointer* to a function can be passed as a parameter to another function.

A function that takes an argument of function type is referred to as a *higher-order* function. Loosely speaking, a higher-order function is a computation parameterized by another computation. We show the power of this feature with a simple example. The function “`sort`”, shown below, takes a list of numbers and sorts them in ascending order. On non-empty arguments, the function “`sort`” recursively sorts the tail and inserts the head at the

right place in the sorted tail. This algorithm becomes inefficient as lists grow longer, but it is easy to understand [\[Browse Program\]](#)[\[Download Program\]](#):

```
sort [] = []
sort (x:xs) = insert x (sort xs)

insert x [] = [x]
insert x (y:ys) | x <= y = x : y : ys
                 | otherwise = y : insert x ys
```

To sort a list in descending order or to sort a list of a different type, a new function must be coded.

An alternative is to code a sort function where the ordering criterion is an argument. The overall structure of the function is the same. The new argument, the first one of each function, is denoted by “f”. This argument is a function that takes two arguments and returns “True” if and only if the first argument must appear before the second argument in the output list [\[Browse Program\]](#)[\[Download Program\]](#):

```
sort _ [] = []
sort f (x:xs) = insert f x (sort f xs)

insert _ x [] = [x]
insert f x (y:ys) | f x y = x : y : ys
                  | otherwise = y : insert f x ys
```

For example:

```
H0InsertionSort> sort (<=) [3,5,1,2,6,8,9,7]
[1,2,3,5,6,7,8,9]
H0InsertionSort> sort (>) [3,5,1,2,6,8,9,7]
[9,8,7,6,5,3,2,1]
```

In the above expressions, the operators “<=” and “>” are the functional arguments. The parentheses around them are necessary, since these functions are identified by infix operators. Without parentheses, the expression “sort <= [3,5,1,2,6,8,9,7]” would test whether the left argument of “<=” is smaller than the right argument, which is meaningless.

Observe that the first version of the “sort” function constrains the elements of the input list to be numbers, since these elements are arguments of “<=” . In the second, higher-order version, the type of the elements of the input list is unconstrained. Thus, the function can be applied to lists of any type as long as a suitable ordering criterion for the type of the list elements is provided.

Higher-order computations involve a functional argument. Sometimes, the corresponding argument in a call, which is a function, is referenced only in the call itself. In this case, it is appropriate to use an anonymous function. For example, suppose that an elementary school information system represents classes with a grade and a section. The grade is a number in the range 1 through 5 and the section is a letter, a, b ... The following ordering criterion sorts the classes in a “natural” (lexicographic) order [\[Browse Program\]](#)[\[Download Program\]](#):

```
sortClasses xs = sort lex xs
  where lex (x,y) (u,v) = x<u || x==u && ord y <= ord v
```

A more compact and informative formulation uses an anonymous function as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
sortClasses xs = sort (\(x,y) (u,v) -> x<u || x==u && ord y <= ord v) xs
```

Observe that pattern matching is normally used in the definition of the above anonymous function.

## 3.12 Lazy Evaluation

The *evaluation* of an expression  $t$  is the process of obtaining a value  $v$  from  $t$ .

A *value* is an expression consisting only of builtin literals and/or data constructors and/or variables.

The value  $v$  is obtained from  $t$  by replacing an instance of the left-hand side of a rule with the corresponding instance of the right-hand side. For example, referring to the function *square* defined in Section 3.5.1:

```
square x = x * x
```

an instance of *square*  $x$  is replaced with the corresponding instance of  $x * x$ . For example,  $4 + \text{square } (2 + 3)$  is replaced by  $4 + (2 + 3) * (2 + 3)$ .

The evaluation of an expression  $t$  proceeds replacement after replacement until an expression  $v$  in which no more replacements are possible is obtained. If  $v$  is not a value, the evaluation fails, otherwise  $v$  is the result of a computation of  $t$ . For example, the following function *head* computes the first element of a (non-null) list:

```
head (x:_) = x
```

An attempt to evaluate “`head []`” fails, since no replacement is possible and the expression is not a value since it contains a function.

Often, an expression may contain several distinct replaceable subexpressions, e.g., from  $(2 + 3) * (2 + 3)$  we can obtain both  $5 * (2 + 3)$  and  $(2 + 3) * 5$ . Even a single subexpression may allow several distinct replacements when non-deterministic functions are involved. The order in which different subexpressions of an expression are replaced is not determined by a program. The choice is made by an evaluation *strategy*. The semantics of the language guarantees that any value obtainable from an expression is eventually obtained. This property is referred to as the *completeness* of the evaluation. To ensure this completeness, expressions must be evaluated lazily. A lazy strategy is a strategy that evaluates a subexpression only if its evaluation is unavoidable to obtain a result. The following example clarifies this delicate point.

The following function computes the list of all the integers beginning with some initial value  $n$  [\[Browse Program\]](#)[\[Download Program\]](#):

```
from n = n : from (n+1)
```

An attempt to evaluate “from 1” aborts with a memory overflow since the “result” would be the infinite term:

```
[1,2,3,...
```

However, the function “from” is perfectly legal. The following function returns the  $n$ -th element of a list:

```
nth n (x:xs) = if n==1 then x else nth (n-1) xs
```

The expression “nth 3 (from 1)” evaluates to 3 despite the fact that “from 1” has no (finite) value:

```
lazy> nth 3 (from 1)
3
```

The reason is that only the third element of “from 1” is needed for the result. All the other elements, in particular the infinite sequence of elements past the third one, do not need to be evaluated.

Infinite data structures are an asset in the conjunction with lazy evaluation. Programs that use infinite structures are often simpler than programs for the same problem that use finite structures. E.g., a function that computes a (finite) prefix of “[1,2,3,...” is more complicated than “from”. Furthermore, the functions of the program are less interdependent and consequently more reusable. E.g., the following function, initially applied to 0 and 1, computes the (infinite) sequence of the Fibonacci numbers:

```
fibolist x0 x1 = x0 : fibolist x1 (x0+x1)
```

The function “nth” can be reused to compute the  $n$ -th Fibonacci number through the evaluation of the expression “nth  $n$  (fibolist 0 1)”, e.g.:

```
lazy> nth 5 (fibolist 0 1)
3
```

The evaluation strategy of the **PAKCS** compiler/interpreter, which is used for all our examples, is lazy, but incomplete. The strategy evaluates non-deterministic choices sequentially instead of concurrently.

All the occurrences of same variables are shared. This design decision has implications both on the efficiency and the result of a computation. For example, consider again the following definition:

```
square x = x * x
```

The evaluation of say `square t` goes through  $t*t$ . Without sharing,  $t$  would be evaluated twice, each evaluation independent of the other. If  $t$  has only one value, the double evaluation would be a waste. If  $t$  has more than one value, this condition will be discussed in Section 3.13.1, sharing produces the same value for both occurrences.

### 3.13 Local Definitions

The syntax of Curry implicitly associates a scope to each identifier, whether a function, a type, a variable, etc. Roughly speaking the scope of an identifier is where in a program the identifier can be used. For example, the scope of a variable occurring in the left-hand side of a rule is the rule itself, which includes the right-hand side and the condition, if any. In the following code:

```
square x = x * x

cube    x = x * square x
```

the variable identified by “x” in the definition of “square” is completely separated from the variable identified by “x” as well in the definition of “cube”. Although these variables share the same name, they are completely independent of each other.

Curry is *statically scoped*, which means that the scope of an identifier is a static property of a program, i.e., the scope depends on the textual layout of a program rather than on an execution of the program.

The *scope* of an identifier is the region of text of a program in which the identifier can be referenced.

In most cases, the programmer has no control on the scope of an identifier—and this is a good thing. The scope rules are designed to make the job of the programmer as easy and safe as possible. The context in which an identifier occurs determines the identifier’s scope. However, there are a couple of situations where the programmer can limit, by means of syntactical constructs provided by the language, the scope of an identifier. Limiting the scope of an identifier is convenient in some situations. For example, it prevents potential name clashes and/or it makes it clearer that a function is introduced only to simplify the definition of another function. A limited scope, which is referred to as a *local scope*, is the subject of this section.

Curry has two syntactic constructs for defining a local scope: the “**where**” clause and the “**let**” clause. They are explained next.

#### 3.13.1 Where Clauses

A “**where**” clause creates a scope nested within a rewrite rule. The following example defines an infix operator, “**\*\***”, for integer exponentiation [[Browse Program](#)][[Download Program](#)]:

```
infixl 8 **

a ** b | b >= 0 = accum 1 a b
      | otherwise = accum aux (y * y) (z ‘div’ 2)
      where aux = if (z ‘mod’ 2 == 1) then x * y else x
```

For example,  $2^{**}5 = 2^5 = 32$ . There are several noteworthy points in the above code fragment. The scope of the function “accum” is limited to the rewrite rule of “\*\*”. This

is convenient since the purpose of the former is only to simplify the definition of the latter. There would be no gain in making the function “`accum`” accessible from other portions of a program. The function “`accum`” is *nested* inside the function “`**`”, which is *nesting* “`accum`”.

The rewrite rule defining “`accum`” is conditional. Pattern matching of the arguments and non-determinism can occur as well in local scopes. Finally, there is yet another local scope nested within the rewrite rule of the function “`accum`”. The identifier “`aux`” is defined in this scope and can be referenced from either condition or right-hand side of the rewrite rule of the function “`accum`”.

The right-hand side of the rewrite rule defining “`aux`” references the variables “`x`”, “`y`” and “`z`” that are arguments of “`accum`” rather than “`aux`” itself. This is not surprising since the scope of these variables is the rewrite rule of “`accum`” and “`aux`” is defined within this rule.

The identifier “`aux`” takes no arguments. Because it occurs in a local scope, “`aux`” is considered a local *variable* instead of a *nullary function*. The language does not make this distinction for non-local identifiers, i.e., identifiers defined at the top level. The evaluation of local variables differs from that of local functions. All the occurrences of a variable, whether or not local, share the same value. This policy may affect both the efficiency of a program execution and the result of computations involving non-deterministic functions. The following example clarifies this subtle point [[Browse Program](#)][[Download Program](#)]:

```
coin = 0
coin = 1

g = (x,x) where x = coin

f = (coin,coin)
```

The values of “`g`” are (0,0) and (1,1) only, whereas the values of “`f`” also include (0,1) and (1,0). The reason of this difference is that the two occurrences of “`coin`” in the rule of “`f`” are evaluated independently, hence they may have different values, whereas the two occurrences of “`x`” in the rule of “`g`” are “shared,” hence they have the same value.

There is one final important aspect of local scoping. A local scope can declare an identifier already declared in a nesting scope—a condition referred to as *shadowing*. An example of shadowing is shown below:

```
f x = x where x = 0
```

The variable “`x`” introduced in the **where** clause *shadows* the variable with the same name introduced in the rewrite rule left-hand side. The occurrence of “`x`” in the right-hand side is bound to the former. Hence, the value “`f 1`” is 0. This situation may be a source of confusion for the beginner. The **PAKCS** compiler/interpreter detects this situation and warns the programmer as follows [[Browse Program](#)][[Download Program](#)]:

```
Prelude> :l shadow
...
shadow.curry, line 1.3: Warning:
  Unused declaration of variable ‘x’
```

```
shadow.curry, line 1.15: Warning:
  Shadowing symbol 'x', bound at: shadow.curry, line 1.3
```

The second warning reports that the identifier in line 1, column 15, the variable “x” in the local scope, shadows some identifier(s) with the same name. The first warning reports that the identifier in line 1, column 3, the variable “x” argument of “f”, is not used. This is a consequence of its shadowing and gives an important clue that the occurrence of “x” in the right-hand side of the rewrite rule of “f” is bound to the local variable rather than the argument.

### 3.13.2 Let Clauses

A “let” clause creates a scope nested within an expression. The concept is very similar to a “where” clause, but the granularity of the scope is finer. For example, the program for integer exponentiation presented earlier can be coded using “let” clauses as well [[Browse Program](#)][[Download Program](#)]:

```
infixl 8 **

a ** b | b >= 0 =
  let accum x y z | z == 0      = x
                    | otherwise =
                        let aux = if (z `mod` 2 == 1) then x * y else x
                            in accum aux (y * y) (z `div` 2)
  in accum 1 a b
```

Using a “let” declaration is more appropriate than a “where” declaration for the definition of operation “aux”. With a “let” declaration, the scope of the identifier “aux” is the right-hand side of the second conditional rule of the function “accum” instead of the whole rule.

### 3.13.3 Layout

By contrast to most languages, Curry programs do not use a printable character to separate syntactic constructs, e.g., one rewrite rule from the next. Similar to Haskell, Curry programs use a combination of an end-of-line and the indentation of the next line, if any. A Curry construct, e.g., a “data” declaration or a rewrite rule, terminates at the end of a line, unless the following line is more indented. For example, consider the following layout:

```
f = g
  h...
```

Since “f” starts in column 1 and “h” starts in column 2, the right-hand side of the rule defining “f” consists in the application of “g” to “h” to “...” By contrast, with the following layout:

```
f = g
h...
```

the right-hand side of the rule defining “f” consists of “g” only. Since “h” starts in the same column as “f”, this line is intended as a new declaration.

The layout style described above goes under the name “off-side rule”. The examples of Sections 3.13.1 and 3.13.2 shows how the off-side rule applies to “**where**” and “**let**” clauses.

## 3.14 Variables

Most of the programs discussed so far are functional. They declare data and/or define functions. An execution of the program is the functional-like evaluation of an expression. Curry is a *functional logic* programming language. It adds two crucial features to the model outlined above: non-determinism, which was discussed in Section 3.5.4, and *logic variables*, which are discussed in this section.

### 3.14.1 Logic Variables

A logic variable differs from the variables introduced by the left-hand side of a rewrite rule. A variable introduced by the left-hand side of a rewrite rule, also called *pattern variable*, stands for any expression (of an appropriate type). For example, the following definition:

```
head (x:xs) = x
```

is read as “for all expressions  $x$  and  $xs$  the head of (the list)  $(x:xs)$  is  $x$ .” Since Curry is strongly typed, the type of  $xs$  must be list, otherwise the program would be invalid, but no other conditions are imposed on  $xs$ .

A *logic variable* either is a variable occurring in an expression typed by the user at the interpreter prompt or it is a variable in the condition and/or right-hand side of a rewrite rule which does not occur in the left-hand side. We show an example of both. The operation “==”, called *Boolean equality*, is predefined in Curry. Hence, one can (attempt to) evaluate:

```
Prelude> z==2+2 where z free
```

Every variable in a query, such as “ $z$ ” in the above example, is a logic variable that initially is not bound to any value. We will discuss shortly why queries with variables may be useful and how variables are handled.

The second kind of logic variable is shown in the following example:

```
path a z = edge a b && path b z   where b free
```

The intuition behind the names tells that in a graph there exists a path from a node  $a$  to a node  $z$  if there exists an edge from the node  $a$  to some node  $b$  and a path from the node  $b$  to the node  $z$ . In the definition, both “ $a$ ” and “ $z$ ” are ordinary (rule) variables, whereas “ $b$ ” is a logic variable. Variables, such as “ $b$ ”, which occur in the condition and/or right-hand side of a rule, but not in the left-hand side, are also called *extra variables*. Extra variables are explicitly declared “**free**” in a “**where**” or “**let**” clause as shown in the example, or are anonymous.

### 3.14.2 Evaluation

The evaluation of expressions containing logic variables is a delicate issue and the single most important feature of functional logic languages. There are two approaches to deal with the evaluation of expressions containing logic variables: *residuation* and *narrowing*.

Let  $e$  be an expression to evaluate and  $v$  a variable occurring in  $e$ . Suppose that  $e$  cannot be evaluated because the value of  $v$  is not known. Residuation suspends the evaluation of  $e$ . If it is possible, we will address this possibility shortly, some other expression  $f$  is evaluated in hopes that the evaluation of  $f$  will bind a value to  $v$ . If and when this happens, the evaluation of  $e$  resumes. If the expression  $f$  does not exist,  $e$  is said to *flounder* and the evaluation of  $e$  fails. For example, this is what would happen for the query we showed earlier:

```
Prelude> z == 2+2 where z free
*** Warning: there are suspended constraints (for details: ":set +suspend")
```

By contrast to residuation, if  $e$  cannot be evaluated because the value of  $v$  is not known, narrowing guesses a value for  $v$ . The guessed value is uninformed except that only values that make it possible to continue the computation are chosen.

The operation “`:=`”, called *constrained equality*, is predefined in Curry. This operation is similar to the Boolean equality discussed earlier except that it returns only `True` (if the equality can be satisfied) or it fails, i.e., it does not return `False` if both sides are not evaluable to identical values. Since this operation succeeds only if both sides have identical values, it also binds logic variables if this is necessary to make the sides identical. Thus:

```
Prelude> z := 2+2 where z free
{z=4} True
```

Therefore, this operation can be used to express an equational constraint that must be satisfied to compute some result.

### 3.14.3 Flexible vs. Rigid Operations

Operations that residuate are called *rigid*, whereas operations that narrow are called *flexible*. All defined operations are flexible whereas most primitive operations, like arithmetic operations, are rigid since guessing is not a reasonable option for them. For example, the prelude defines a list concatenation operation as follows:

```
infixr 5 ++
...
(++): [a] -> [a] -> [a]
[] ++ ys = ys
(x:xs) ++ ys = x : xs ++ ys
```

Since the operation “`++`” is flexible, we can use it to search for a list satisfying a particular property:

```
Prelude> xs ++ [3,4] := [1,2,3,4] where xs free
{xs=[1,2]} True
```

On the other hand, predefined arithmetic operations like the addition “+” are rigid. Thus, a call to “+” with a logic variable as an argument flounders:

```
Prelude> x + 2 := 4 where x free
*** Warning: there are suspended constraints (for details: ":set +suspend")
```

For *ground expressions*, i.e., expressions without logic variables, the flex/rigid status of a function makes no difference. In the context of concurrent/distributed object-oriented programming, rigid user-defined functions can be useful. For this purpose, there is a primitive operation `ensureNotFree` that evaluates its argument and suspends if it is a logic variable.

### 3.14.4 Programming

Often, programming with variables leads to conceptually simple, terse and elegant code at the cost of an acceptable loss of efficiency. The logic variables of a program and/or a query are not much different from the variables that are typically used to solve algebra or geometry problems. In both cases, some unknown entities of the problem are related to each other by expressions involving functions. Narrowing allows us to evaluate these expressions—and in the process to find values for the variables. The simplest application, and the most familiar for those used to solve algebra and geometry problems with variables, is when the expression to evaluate is an equation.

In later chapters, we will discuss some problems that are conveniently solved if one uses variables in computations. Here we want to present a simple, but non-trivial, motivating example. The problem is to parse a string that represents an expression. To keep the example small, our expressions are functional terms whose syntax is defined by:

```
term      ::= identifier
           | identifier '(' args ')'
args      ::= term
           | term ',' args
identifier ::= any non-null string of alphabetic characters
```

For example, “`f(g(a,b))`” is a term described by the above syntax. When a term is represented as a string, answering questions such as how many arguments “`g`” has, is more complicated and less efficient than it needs to be. A parser converts a term from its string representation into a data structure that makes easy and efficient answering questions of that kind. Thus, the first step to build a parser is to design a suitable type to represent a term. Our choice is: [\[Browse Program\]](#)[\[Download Program\]](#):

```
data Term = Term String [Term]
```

Note that the occurrence of “`Term`” to right of the “`=`” character is a data constructor, whereas the two other occurrences are type constructors. The “`Term`” identifier is *overloaded* by the declaration.

Using this data structure, we represent a function identifier with a string and the function’s arguments with a list of terms. For example, the term “`f(g(a,b))`” would be represented as “`Term "f" [Term "g" [Term "a" [],Term "b" []]]`”. The following operation parses

a term [\[Browse Program\]](#)[\[Download Program\]](#):

```
parseTerm (fun++("++args++")) | all isAlpha fun = Term fun (parseArgs args)
parseTerm s | all isAlpha s = Term s []
```

The elements of the program relevant to our discussion are the variables “fun” and “args”. The functional pattern in the first rule acts similarly to solving the equation “s := fun++(“++args++”)” in which “s” is the argument of “parseTerm”. The first condition of the first rule of the operation “parseTerm” instantiates these variables and ensures that “fun” is an alphabetic identifier. The operation “isAlpha”, defined in the library “Data.Char”, ensures that its argument, a character, is alphabetic. The operation “all” is defined in the “Prelude”. The combination “all isAlpha” ensures that all the characters of a string are alphabetic.

If a term has arguments, these arguments are parsed by the operation “parseArgs”. The overall design of this operation is very similar to that of “parseTerm”. In this case, though, a string is decomposed according to different criteria [\[Browse Program\]](#)[\[Download Program\]](#):

```
parseArgs (term++", "++terms) = parseTerm term : parseArgs terms
parseArgs s = [parseTerm s]
```

One could code more efficient versions of this parser. This version is very simple to understand and it is the starting point for the design of more efficient versions that will be discussed later in this book.

### 3.15 Input/Output

As we have seen up to now, a Curry program is a set of datatype and function declarations. Functions associate result values to given input arguments. However, application programs must also interact with the “outside” world, i.e., they must read user input, files etc. Traditional programming languages address this problem by procedures with side effects, e.g., a procedure `read` that returns a user input when it is evaluated. Such procedures are problematic in the context of Curry. Firstly, the evaluation time of a function is difficult to control due to the lazy evaluation strategy (see Section 3.12). Secondly, the meaning of functions with side effects is unclear. For instance, if the function `readFirstNum` returns the first number in a particular file, the evaluation of the expression “`2*readFirstNum`” yields different values at different points of time (if the contents of the file changes).

Curry solves this problem with the “monadic I/O” concept much like that seen in the functional language Haskell [23]. In the monadic approach to I/O, a program interacting with the outside world is considered as a sequence of actions that change the state of the outside world. Thus, an interactive program computes actions which are applied to a given state of the world (this application is finally done by the operating system that executes a Curry program). As a consequence, the outside world is not directly accessible but can be only manipulated through actions that change the world. Conceptually, the world is encapsulated in an abstract datatype which provides actions to change the world. The type of such actions is “IO t” which is an abbreviation for

```
World -> (t,World)
```

where “World” denotes the type of all states of the outside world. If an action of type “IO t” is applied to a particular world, it yields a value of type t and a new (changed) world.

For instance, `getChar` of type “IO Char” is an action which reads a character from the standard input whenever it is executed, i.e., applied to a world. Similarly, `putChar` of type “Char -> IO ()” is an action which takes a character and returns an action which, when applied to a world, puts this character to the standard output (and returns nothing, i.e., the unit type). The important point is that values of type `World` are not accessible to the programmer — she/he can only create and compose actions on the world.

Actions can only be sequentially composed, i.e., one can build a new action that consists of the sequential evaluation of two other actions. The predefined function

```
(>>) :: IO a -> IO b -> IO b
```

takes two actions as input and yields an action as the result. The resulting action consists of performing the first action followed by the second action, where the produced value of the first action is ignored. For instance, the value of the expression “`putChar 'a' >> putChar 'b'`” is an action which prints “ab” whenever it is executed. Using this composition operator, we can define a function `putStrLn` (which is actually predefined in the prelude) that takes a string and produces an action to print this string:

```
putStrLn []      = putChar '\n'  
putStrLn (c:cs) = putChar c >> putStrLn cs
```

If two actions should be composed and the value of the first action should be taken into account before performing the second action, the actions can be also composed by the predefined function

```
(>>=) :: IO a -> (a -> IO b) -> IO b
```

where the second argument is a function taking the value produced by the first action as input and performs another action. For instance, the action

```
getChar >>= putChar
```

is of type “IO ()” and copies, when executed, a character from standard input to standard output. Actually, this composition operator is the only elementary one since the operator “>>” can be defined in terms of “>>=”:

```
a1 >> a2 = a1 >>= \_ -> a2
```

There is also a primitive “empty” action

```
return :: a -> IO a
```

that only returns the argument without changing the world. Thus, one can define an “empty” action which returns nothing (i.e., the unit type) as

```
done :: IO ()
```

```
done = return ()
```

Using these primitives, we can define more complex interactive programs. For instance, an I/O action that copies all characters from the standard input to the standard output up to the first period can be defined as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
echo = getChar >>= \c -> if c=='.' then return ()
                        else putChar c >> echo
```

Obviously, such a definition is not well readable. Therefore, Curry provides a special syntax extension for writing sequences of I/O actions, called the *do notation*. The do notation follows the layout style (see Section 3.13.3), i.e., a sequence of actions is vertically aligned so that

```
do putChar 'a'
   putChar 'b'
```

is the same as “putChar 'a' >> putChar 'b'”, and

```
do c <- getChar
   putChar c
```

is just another notation for “getChar >>= \c -> putChar c”. Thus, the do notation allows a more traditional style of writing interactive programs. For instance, the function `echo` defined above can be written in the do notation as follows:

```
echo = do c <- getChar
         if c=='.'
         then return ()
         else do putChar c
                echo
```

As a further example, we show the definition of the I/O action `getLine` as defined in the prelude. `getLine` as an action that reads a line from the standard input and returns it:

```
getLine :: IO String
getLine = do c <- getChar
           if c=='\n'
           then return []
           else do cs <- getLine
                  return (c:cs)
```

Curry also provides predefined I/O actions for reading files and accessing other parts of the environment. For instance, “`readFile f`” is an action which returns the contents of file `f` and “`writeFile f s`” is an action writing string `s` into the file `f`. This allows us to define a function that copies a file with transforming all letters into uppercase ones in a very concise way (`toUpper` is defined in the standard character library `Data.Char` and converts lowercase into uppercase letters) [\[Browse Program\]](#)[\[Download Program\]](#):

```
convertFile input output = do
  s <- readFile input
  writeFile output (map toUpper s)
```

The function `toUpper`, defined in the library “`Data.Char`”, takes a character. If the character is lower case and alphabetic, then it returns it in upper case, otherwise it returns it unchanged. The operation “`map`” is defined in the “`Prelude`” and discussed in detail in Section 4.2.6. The combination “`map toUpper`” transforms all the characters of a string to upper case.

The monadic approach to input/output has the advantage that there are no “hidden” side effects—any interaction with the outside world can be recognized by the `IO` type of the function. Thus, functions can be evaluated in any order and the only way to combine I/O actions is a sequential one, as one would expect also in other programming languages. However, there is one subtle point. If a function computes non-deterministically different I/O actions, like in the expression “`putStrLn (show coin)`” (see Section 3.13.1 for the definition of the non-deterministic function `coin`; `show` is a predefined function that converts any value into a string), then it is not clear which of the alternative actions should be applied to the world. Therefore, Curry requires that *non-determinism in I/O actions must not occur*. For instance, we get a run-time error if we evaluate the above expression:

```
localvar> putStr (show coin)
ERROR: non-determinism in I/O actions occurred!
```

One way to ensure the absence of such errors is the encapsulation of all search between I/O operations, e.g., by using set functions.

**Exercise 6** Define an I/O action `fileLength` that reads the name of a file from the user and prints the length of the file, i.e., the number of characters contained in this file. [\[Browse Answer\]](#)[\[Download Answer\]](#)

## Part II

# Programming with Curry

# Chapter 4

## Programming in Curry

### 4.1 Overview

*Lists* and *trees* are datatypes frequently used in programming.

- A *list* abstracts a sequence of elements. The elements of a list are implicitly ordered by the list structure. Therefore, a list is a convenient representation for queues, stacks and other linear structures. As list can also be used for representing collections, typically unordered, such as a set, by ignoring or hiding the implicit order of the elements.
- A *tree* is a multibranching data structure that abstracts a hierarchy of values or conditions. It naturally represents taxonomies or classifications and therefore it is useful for problems involving search. Trees come in many variants, but all consists of a value called *root* and some subtrees called *children*. Similar to lists, trees can be used for representing collections.

This section describes in some detail both these datatypes and how they help solve some typical problems, e.g., sorting a collection of elements or searching for an element in a collection.

### 4.2 Lists

#### 4.2.1 Notation

A *List* is a simple algebraic polymorphic datatype defined by two constructors conventionally referred to as *Nil* and *Cons*. Within the Curry language, the datatype “*List of a*” would be declared as:

```
data List a = Nil | Cons a (List a)
```

Because lists are one of the most frequently used types in functional, logic and functional logic programs, many languages offer several special notations for lists. In Curry, the type “*List of a*”, where *a* is a type variable that stands for any type, is predefined and denoted by `[a]`. Likewise, `[]` denotes the constructor *Nil*, the empty list, and “`:`” denotes the constructor *Cons*, which takes an element of type `a` and a list of `a`'s. Thus, with a syntax that is *not* legal in Curry, but is quite expressive, the above declaration would look like:

```
data [a] = [] | a : [a]
```

The expression  $(u:v)$  denotes the list with the first element  $u$  followed by the list  $v$ . The infix operator “:”, which read “cons”, is predefined, right associative and has precedence 5. This implies that  $u:v:w$  is parsed as  $u:(v:w)$ .

A list can also be denoted by enumerating its elements, e.g., “[ $u,v,w$ ]” is a list containing three elements, “ $u$ ”, “ $v$ ” and “ $w$ ”, i.e., it is just another notation for “ $u:v:w:[]$ ”. This notation can be used with any number of elements. The elements are enclosed in brackets and separated by commas. This notation has several advantages over the standard algebraic notation: lists stand out in a program and references to lists are textually shorter. In particular, the number of parentheses occurring in the text is reduced. This claim can be easily verified by comparing the built-in notation with the ordinary notation.

The type list is polymorphic, which means that different lists can have elements of different types. However, all the elements of a particular list must have the same type. The following annotated examples show this point [\[Browse Program\]](#)[\[Download Program\]](#):

```
-- list of integers
digits = [0,1,2,3,4,5,6,7,8,9]

-- list of characters, equivalent to "Pakcs", print with putStr
string = ['P','a','k','c','s']

-- list of list of integers
matrix = [[1,0,2],[3,7,2],[2,8,1],[3,3,4]]
```

Other special notations available for lists are described in Sections [4.2.3](#) and [4.2.4](#).

## 4.2.2 Inductive Definitions

Many elementary functions on lists are defined by an induction similar to that available for the naturals. The cases of the induction are conveniently defined by different rules using pattern matching. For lists, the base case involves defining a function for  $[]$  whereas the inductive case involves defining the function for a list  $(u:v)$  under the assumption that the value of the function for  $v$  is available. In a program, this is expressed by a recursive call. The function that counts the number of elements of a list is emblematic in this respect:

```
len []      = 0
len (u:v)  = 1 + len v
```

For computing the length of a list, the value of  $u$  is irrelevant and  $u$  should be replaced by an anonymous variable in the above definition.

**Exercise 7** Code an inductively defined function that takes a list of integers and returns the sum of all the integers in the list. Hint: the function should return 0 for an empty list.

[\[Browse Answer\]](#)[\[Download Answer\]](#)

The prelude defines many useful functions on lists, e.g., “++” for concatenation, “!!” for indexing, i.e.,  $(l!!i)$  is the  $i$ -th (starting from 0) element of  $l$ , etc. We will use some of these

functions, after providing a brief explanation, in this section. We might also re-define some functions already available in the prelude or other libraries when they make good examples. E.g., the function `len` discussed above is equivalent to the function `length` of the prelude. In Section 4.2.5, we will present the most important list functions available in the prelude.

Functions inductively defined are easy to code, understand and evaluate. Sometimes they may be inefficient. Below are two definitions of a function to reverse a list. For long lists, the second one is much more efficient.

```
slowRev [] = []
slowRev (u:v) = slowRev v ++ [u]

fastRev l = aux l []
  where aux [] r = r
        aux (u:v) r = aux v (u:r)
```

A function inductively defined performs a “traversal” of its argument. During this traversal some computation is performed on each element of the list—this is referred to *visiting* a *cons*—and the result combined with a recursive invocation of the function. Loosely speaking, the visit can be performed either *before* the recursive call, or *after*, or *both*. The following example shows how to subtract the minimum element of a list of integers from all the elements of the list. The function performs a single traversal of its argument. The minimum of the list is computed (as much as feasible) before the recursive call. The subtraction is computed after the recursive calls (otherwise the minimum could not be known) [[Browse Program](#)][[Download Program](#)]:

```
submin [] = []
submin (x:xs) = fst (aux (x:xs) x)
  where aux [] m = ([],m)
        aux (y:ys) m = let (zs,n) = aux ys (min y m)
                        in (y-n:zs,n)
```

The function `fst`, which returns the first element of a pair, is defined in the prelude. The function `min`, which returns the minimum of two integers, is defined in the standard prelude.

More complicated computations may lead to more complicated inductive definitions. A discussion on the structure and the design of inductively defined function is in [1].

**Exercise 8** Code an inductively defined function that transposes a matrix represented by a list of lists (all of the same length). [[Browse Answer](#)][[Download Answer](#)]

There are a couple of noteworthy alternatives to directly defining inductive functions. One involves higher-order list functions. Some of these functions are presented in Section 4.2.6. The other involves narrowing. Lists are a particularly fertile ground for narrowing. Below are two definitions of the function that computes the last element of a list. The first definition is inductive, whereas the second is narrowing-based.

```
inductLast [x] = x
inductLast (x:y:z) = inductLast (y:z)

narrowLast (_++[e]) = e
```

Observe that `narrowLast` computes the result by solving the equation “`1 == _++[e]`” in which “`1`” is the argument of the call.

### 4.2.3 Ranges

A special notation is available to define lists containing *ranges* of integers. The most common of this notation is “`[e1 .. e2]`” which denotes the list “`[e1, e1 + 1, e1 + 2, ..., e2]`”. For example:

```
Prelude> [2..5]
Result: [2,3,4,5] ?
Prelude>
```

Similarly, the expression “`[e ..]`” denotes the *infinite* list of all the integers starting from *e*. This list cannot be printed in its entirety, but it can be used in a program if only a finite portion of the list is needed, because the evaluation strategy is lazy.

The elements in the lists defined by the above expressions are consecutive, i.e., the distance between adjacent elements is one. The above expressions can be generalized to produce lists where the distance between adjacent elements is a constant greater than one. This distance is inferred from the first two elements of the expression. For example:

```
Prelude> [2,6..20]
Result: [2,6,10,14,18] ?
Prelude>
```

Likewise, “`[2, 6 ..]`” generates the infinite list “`[2,6,10,14,...]`”.

Ranges can be defined using ordinary functions. The prelude defines four functions whose names start with `enumFrom`. These functions define in the ordinary syntax the notations for ranges.

### 4.2.4 Comprehensions

Another useful notation involving lists goes under the name of *list comprehension*. A list comprehension is a notation to construct a list from one or more other lists called *generators*. It goes without saying that ranges are simple generators. For example, the infinite sequence of square and triangular numbers are obtained as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
squares = [x * x | x <- [0 ..]]
triangles = [x * (x+1) 'div' 2 | x <- [0 ..]]
```

A *generator* is an expression of the form `var <- list`. Generators can be nested and/or combined with *guards*. A *guard* is a Boolean expression that filters the elements produced by the generator. For example, if `isPrime` is a predicate telling whether an integer greater than 2 is a prime number, the following comprehension is the sequence of the prime numbers [\[Browse Program\]](#)[\[Download Program\]](#):

```
primes = [x | x <- [2 ..], isPrime x]
```

In this example, the guard is the Boolean expression (`isPrime x`). The elements produced by the generator are passed to the comprehension if and only if the guard holds.

Generators are considered to be nested from left to right. The following example shows how to compute pairs where the second component is not greater than the first [\[Browse Program\]](#)[\[Download Program\]](#):

```
lexPairs = [(x,y) | x <- [0 .. 3], y <- [x .. 3]]
```

This simple example shows that the second generator (`y<-[x .. 3]`) is nested within the first one, since it references the generated elements.

**Exercise 9** Compute the Fibonacci sequence using a list comprehension. Hint: compute a list of *pairs* of numbers where each pair contains two *consecutive* Fibonacci numbers. [\[Browse Answer\]](#)[\[Download Answer\]](#)

#### 4.2.5 Basic Functions

The **PAKCS** compiler/interpreter of Curry is distributed with the prelude, a collection of primitive and fundamental types and functions, and with several libraries. The prelude and some of these libraries contain useful list functions. In this section, we informally discuss some of these functions. The `currydoc` documentation utility, which is distributed with **PAKCS**, should be used for an exhaustive up-to-date consultation of the content of these libraries.

Name	Description	Example(s)
<code>head</code>	First element of a list	<code>head [1,2] = 1</code> ; <code>head []</code> fails
<code>tail</code>	All the elements but the first	<code>tail [1,2] = [2]</code> ; <code>tail []</code> fails
<code>length</code>	Length	<code>length [1,2] = 2</code>
<code>null</code>	Tell whether it is nil	<code>null [1,2] = False</code>
<code>++</code>	Concatenate two lists	<code>[1,2]++[3] = [1,2,3]</code>
<code>!!</code>	$n$ -th element of a list	<code>[1,2]!!1 = [2]</code> ; <code>[1,2]!!4</code> fails
<code>reverse</code>	Reverse the order of the elements	<code>reverse [1,2] = [2,1]</code>
<code>concat</code>	Concatenate all the lists of a list	<code>concat [[1,2],[3]] = [1,2,3]</code>
<code>take</code>	List of the first $n$ elements	<code>take 2 [1,2,3] = [1,2]</code>
<code>drop</code>	All elements but the first $n$	<code>drop 2 [1,2,3] = [3]</code>
<code>and</code>	Boolean conjunction	<code>and [True,False,True] = False</code>
<code>or</code>	Boolean disjunction	<code>or [True,False,True] = True</code>
<code>elem</code>	Whether a value is in a list	<code>elem 2 [1,3,5] = False</code>
<code>nub</code>	Remove duplicates	<code>nub [1,2,2] = [1,2]</code>
<code>delete</code>	Remove the first occurrence of a value	<code>delete 2 [2,1,2] = [1,2]</code> ; <code>delete 2 [1] = [1]</code>

Many more functions that operate on lists are defined in the libraries of the **PAKCS** distribution (e.g., see the library `Data.List` which contains the definition of `nub` and `delete` discussed above). The above table is intended to give only a feeling of what is available.

## 4.2.6 Higher-order Functions

Lists are commonly used to represent collections of elements. Some computations of a list can be expressed by repeatedly applying another, somewhat simpler, computation to all the elements of the collection. This section discusses some frequently occurring situations of this kind.

The simplest case is when a list, which we refer to as the *result list*, is obtained from another list, which we refer to as the *argument list*, by applying the same function, say `f`, to all the elements of the argument list. This is easily accomplished by defining a new function, say `flist` since its analogy to `f`, as follows:

```
flist []      = []
flist (x:xs) = f x : flist xs
```

Although trivial, the definition of `flist` can be avoided altogether using the function `map`, provided by the prelude. The function `map` is higher-order in that it takes as an argument the function, in this example `f`, that is applied to all the arguments of the list. Thus, the function `flist` defined above is the same as `map f`.

The following code, taken from the prelude, shows the type and the definition of `map`:

```
map      :: (a->b) -> [a] -> [b]
map _ [] = []
map f (x:xs) = f x : map f xs
```

It can be seen that the first argument of `map` is a function from any type *a* to any type *b*. The second argument of `map` is a list whose elements must have, of course, type *a*. The result is a list of type *b*. For example, suppose that `isEven` is a function telling whether an integer is even. Then, the expression `(map isEven [0,1,2,3])` evaluates to `[True,False,True,False]`.

A second frequently used higher-order function on lists is `filter`. As the name suggests, `filter` is used to filter the elements of a list that satisfy some criterion expressed by a predicate.

The following code, taken from the prelude, shows the type and the definition of `filter`:

```
filter      :: (a -> Bool) -> [a] -> [a]
filter _ [] = []
filter p (x:xs) = if p x then x : filter p xs else filter p xs
```

It can be seen that the first argument of `filter` is a function from any type *a* to `Bool`, i.e., a predicate. The second argument of `map` is a list whose elements must have, of course, type *a*. The result is again a list of type *a*. The elements of the result are the elements of the second argument that satisfy the predicate. For example, as before, suppose that `isEven` is a function telling whether an integer is even. Then, the expression `(filter isEven [0,1,2,3])` evaluates to `[0,2]`.

The last higher-order function operating on lists that we describe in this section is used to “combine together” all the elements of a list. For example, a function that adds all the elements of a list of integers can be defined using a higher-order function and the ordinary

addition on integers. Several options should be considered, e.g., whether the elements of a list are composed starting with the first or the last one, whether the list can be empty and thus a default value must be supplied, etc. The prelude contains a family of functions, referred to as *folds* for this purpose. The names of these functions starts with “fold”.

The following code, taken from the prelude, shows the type and the definition of `foldr`:

```
foldr          :: (a->b->b) -> b -> [a] -> b
foldr _ z []   = z
foldr f z (x:xs) = f x (foldr f z xs)
```

For example, functions that compute the sum, product and maximum of all the elements of a list of integers are easily defined through `foldr` as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
sumList  = foldr (+) 0
prodList = foldr (*) 1
maxList  = \l -> foldr max (head l) (tail l)
```

The last function is more complicated than the previous two, because it is meaningful only for non-empty lists. The function `foldr1`, defined in the prelude, would simplify our definition of `maxList`.

#### 4.2.7 Set Functions

A non-deterministic function  $f$  may return different results for some combination of arguments. The programmer has no control over which of these results an invocation of  $f$  returns. Any result returned by  $f$  is completely unrelated to any other result. For some problems, it may be convenient to consider *all* the results returned by  $f$  as a whole. The device that returns *all* the results returned by  $f$  for some combination of arguments is called the *set function* of  $f$  and is typically denoted  $f_S$ . For example, given:

```
f x = x ? x+1
```

the value of  $f_S x$  is the set  $\{x, x+1\}$  where the details of the representation of this set are irrelevant to our discussion.

The definition of the set function of a function  $f$  separates the non-determinism of  $f$  from any non-determinism of the arguments to which  $f_S$  is applied [\[6\]](#). In particular,  $f_S$  is deterministic for any  $f$ . Referring to the example above,  $f_S (2 ? 4)$  evaluates to  $\{2, 3\}$  and  $\{4, 5\}$  in which the non-determinism originates entirely from the argument.

To ease the definition of set functions, there is a library `Control.Search.SetFunctions`. This library defines both a suitable abstraction of a type *set* to represent the results of a set function application, and a family of functions `set0`, `set1`, ... Gives a function  $f$  of arity  $n$ , the set function of  $f$  is provided by the expression `setn f`. The first argument of `setn` must be the *identifier* of a function of arity  $n$ .

For example, consider the problem of computing all the subsets of a set  $S$ . This is called the powerset of  $S$ . Let us represent a set with a list. This representation requires some care to ensure that duplicate elements in a list and the order of the elements in a list are not

observable. We ignore these issues since they are irrelevant to our discussion. The following non-deterministic function returns a subset of its argument, a set represented as a list [\[Browse Program\]](#)[\[Download Program\]](#):

```
subset []      = []
subset (x:xs) = x:subset xs
subset (_:xs) =  subset xs
```

In [PAKCS](#), with the help of the library `Control.Search.SetFunctions`, we define the power set of a set as follows:

```
powerset s = set1 subset s -- powerset is the set function of subset
```

For example, the prerequisites for the undergraduate Computer Science courses at Portland State are abstracted by 16 rules as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
isPrereqOf 162 = 161
isPrereqOf 163 = 162
isPrereqOf 200 = 162
...
isPrereqOf 303 = 252
isPrereqOf 303 = 300
isPrereqOf 350 = 252
```

The meaning is that, e.g., 162 is a direct prerequisite of both 163 and 200 and that, e.g., both 252 and 300 are direct prerequisites of 303. Observe that `IsPrereqOf` is a many-to-many relation.

The function to compute *all* the direct prerequisites of a course is shown below [\[Browse Program\]](#)[\[Download Program\]](#):

```
isPrereqOfS course = set1 IsPrereqOf course
```

## 4.2.8 Narrowing

Narrowing is a convenient programming feature when dealing with lists. Lists are frequently used to represent collections of elements. Sometimes the problem is to find in a list either elements or sublists that satisfy certain relationships. The programmer can either code functions to compute these elements or express the relationships using variables for these elements and let narrowing compute the elements by instantiating the variables. Generally, the latter leads to simpler and more declarative programs.

For example, consider a program that plays the game of poker. A hand is represented by a list of 5 cards. Suppose that the problem is to find whether 4 out of the 5 cards have the same rank, i.e., the hand is a four-of-a-kind. A narrowing-based solution removes one card from the hand so that the remaining 4 cards have the same rank. The following function takes a hand and returns a Maybe type. If the hand is a four-of-a-kind, the function returns *just* the rank of the four cards, otherwise it returns *nothing*. [\[Browse Program\]](#)[\[Download Program\]](#):

```
isFour (x++[_]++z) | map rank (x++z) == [r,r,r,r] = Just r where r free
isFour'default _ = Nothing
```

The card removed from the hand is represented by the anonymous variable in the functional pattern. This card is non-deterministically selected. The remaining cards are represented by  $x$  and  $z$ . Additionally, the condition of the first rule imposes that all the cards in  $x$  and  $z$  have the same rank,  $r$ . The rank, too, is non-deterministically selected by solving the equation “`map rank (x++z) == [r,r,r,r]`”. If the condition succeeds, there is obviously a unique value for all these variables. If the first rule cannot be applied, it must be that there are no four cards of the same rank in the hand. The default rule reports this condition

The advantage of the narrowing-based approach over more conventional approaches is that no instructions need to be coded both to isolate the card that does not contribute to the four-of-a-kind nor to find the rank of the four-of-a-kind when it exists.

The above example is typical of situations in which a collection contains elements that must satisfy a certain conditions. Since lists are implicitly ordered, conditions involving the *position* of elements in a collection can also be conveniently expressed using narrowing.

**Exercise 10** Similar to the example just discussed, code a function that tells whether a hand in a game of poker is a *full house*. Hint: [\[Browse Cards.curry\]](#)[\[Download Cards.curry\]](#) defines suits, ranks, etc. [\[Browse Answer\]](#)[\[Download Answer\]](#).

## 4.3 Trees

We discuss two common variants of trees and show some typical functions of each variant.

### 4.3.1 Binary Search Trees

A *binary tree* is either of the following: a singleton value called *empty* (also *null* or *leaf*) or a pair, called a *branch*, consisting of two binary trees called the *left* and the *right child*. Most often, a branch is a triple rather than a pair which in addition to the children also stores a value of some generic set. This value is called the *root* or *decoration* of the tree.

A (decorated) binary tree is declared in Curry as:

```
data BinTree a = Leaf | Branch a (BinTree a) (BinTree a)
```

where `BinTree` is a *type constructor* and  $a$  is its parameter and stands for the type of the decorations. A popular variant of binary trees is called a *binary search tree*. The set of decorations is totally ordered and the decoration of a non-empty binary search tree is greater than all the decorations in the left child and smaller than all the decorations in the right child. This condition prevents repeated decorations in a binary search tree. The following function inserts a value in a binary search tree in such a way that the result is again a binary search tree [\[Browse Program\]](#)[\[Download Program\]](#):

```
insert x Leaf = Branch x Leaf Leaf
insert x (Branch d l r)
  | x < d = Branch d (insert x l) r
```

```

| x > d = Branch d l (insert x r)
| otherwise = Branch d l r

```

An in-order traversal of any binary search tree produces the sorted list of the decorations of the tree.

```

inorder Leaf = []
inorder (Branch d l r) = inorder l ++ [d] ++ inorder r

```

**Exercise 11** Sort a list without repeated values by constructing a binary search tree from the list and then traversing the tree [\[Browse Answer\]](#)[\[Download Answer\]](#).

### 4.3.2 Trie Trees

An *ordered tree* is a pair in which the first component is an element of a set, called the set of decorations, and the second component is a sequence of ordered trees.

An ordered tree is declared in Curry as:

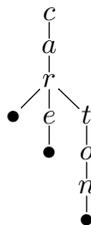
```

data Tree a = Tree a [Tree a]

```

where  $a$  is a parameter that stands for the type of the decorations and the identifier “*Tree*” is overloaded to denote both a type constructor (1st and 3rd occurrences) and a data constructor (2nd occurrence).

A *trie* is a tree that stores a mapping from keys, typically strings, to values and is characterized by sharing key prefixes. We present a simple variant where only keys are stored. This variant is useful to efficiently represent a dictionary and tell whether a string is in the dictionary. For example, a trie storing the strings “car”, “care” and “carton” stores the letter ‘c’, ‘a’, and ‘r’, only once as shown below. The distinguished symbol ‘•’ terminates a string.



We declare the type of a trie as follows:

```

type Trie = [Tree Char]

```

The following function inserts a string in a trie sharing whatever prefix of the string might already be present in the trie. The distinguished symbol that terminates a string is a period.

[\[Browse Program\]](#)[\[Download Program\]](#)

```

insert :: String -> Trie -> Trie
insert []      t = (Tree '.' [] : t)
insert (w:ws) [] = [Tree w (insert ws [])]

```

```
insert (w:ws) (Tree c cs : ts)
  | ord w < ord c = insert (w:ws) [] ++ (Tree c cs : ts)
  | ord w > ord c = Tree c cs : insert (w:ws) ts
  | otherwise     = Tree c (insert ws cs) : ts
```

**Exercise 12** Code functions to build a trie from a list of words and to print all the words in the trie [\[Browse Answer\]](#)[\[Download Answer\]](#).

**Exercise 13** Code a function that takes a word and a trie and tells whether or not the word is in the trie [\[Browse Answer\]](#)[\[Download Answer\]](#).

## Chapter 5

# Managing Curry Packages

There are many libraries and tools for Curry that are not distributed with an available Curry system but can be accessed via the Curry package system. Currently, more than one hundred packages are available. Some of them contain small libraries, others contain quite complex tools, like the Curry preprocessor. The Curry Package Manager (**CPM**), which is part of the Curry systems **PAKCS** and **KICS2**, eases the access and use of these packages. In the following, the basic use of **CPM** is explained. A detailed description of all features of **CPM** can be found in its [user manual](#).

The executable of the Curry Package Manager is named `cypm` and located in the `bin` directory of **PAKCS** or **KICS2**. When you use **CPM** for the first time, execute

```
> cypm update
```

to download a local copy of the index of all available packages. A list of all packages in this index can be shown by the `list` command:

```
> cypm list
Name                Synopsis                Version
----                -
abstract-curry      Libraries to deal with AbstractCurry programs  3.0.0
abstract-haskell    Libraries to represent Haskell programs in Curry 3.0.0
addtypes            A tool to add missing type signatures in a Curry program
...

```

The command

```
> cypm info PACKAGE
```

can be used to show more information about the package with name `PACKAGE`.

### 5.1 Importing Existing Packages

To implement a larger application with Curry, one probably needs many libraries from other packages. In this case, one should write the application as a Curry package so that all required dependencies can be specified so that **CPM** can manage them. This is explained in more detail

in Section 5.3. If one wants to execute a smaller Curry program which uses a library from some Curry package, then one can use CPM's `add` command to add this package as a global dependency and download and install it globally (i.e., in your user-home environment). For instance, the package `pflp` supports probabilistic functional logic programming [9]. It can be installed as a global dependency by the command

```
> cypm add pflp
```

The command

```
> cypm info pflp --all
```

shows all information about this package. In particular, one can see that the module `PFLP` is exported by this package. Thus, one can use this module in a program using probabilistic functional logic programming by adding the line

```
import PFLP
```

in the header of the program. When this program is loaded with `PAKCS`, the load path is set in such a way so that the module `PFLP` from package `pflp` can be imported.

Note that this method to use packages should be used only for small programs or to try some features of a specific package. Actually, each version of each Curry system has its own global package cache.<sup>1</sup> For larger applications, one should install the required packages locally (which is described in Section 5.3 below).

## 5.2 Installing Tools

Many tools for Curry are available as packages. Actually, more than thirty tools are available as packages, e.g., to analyze, test, or verify Curry programs, generate documentation, web frameworks, etc. Such packages provide an “executable” (its name is shown by CPM's `info` command). In order to install a tool provided by `PACKAGE`, one can use the command

```
> cypm install PACKAGE
```

This command downloads the package into some internal directory (`$HOME/.cpm/apps_...`), compiles the tool, and installs the binary of the tool provided by the package in `$HOME/.cpm/bin`. Hence it is recommended to add this directory to your path.

For instance, the most recent version of CPM can be installed by the commands

```
> cypm update
...
> cypm install cpm
... Package 'cpm-xxx' checked out ...
...
INFO Installing executable 'cypm' into '/home/joe/.cpm/bin'
```

---

<sup>1</sup>Use the command `cypm config` and look at `HOME_PACKAGE_PATH` to see the directory of this global cache. If it is no longer needed or should be initialized, one can simply delete this directory.

Now, the binary `cypm` of the most recent **CPM** version can be used if `$HOME/.cpm/bin` is in your path (before the `bin` directory of the Curry system!).

### 5.3 Developing Applications and Packages

If one wants to implement an application in Curry which uses other Curry packages, one should create a *package* for this application in order to specify all dependencies so that they can be managed by **CPM**. The easiest way to create a new package is to use **CPM**'s `new` command with the name of the new package:

```
> cypm new myproject
```

This creates a new directory `myproject` in which the application can be developed. The generated file structure is as follows:

```
myproject
|-- LICENSE
|-- package.json
|-- README.md
|-- src
    |-- Main.curry
```

This represents the minimal structure of a reasonable package (so that it could later be published). The file `README.md` should contain a description of the package in plain text or markdown syntax. The `LICENSE` file is BSD-3 but could be changed. The source code of the package must be stored in directory `src` and might consist of an arbitrary number of modules.

The file `package.json` is the most important one for managing packages. It is a **JSON** file containing the metadata of the package, like its name, version, author, synopsis, etc. The detailed description of all possible metadata fields can be found in **CPM's user manual**. One has to modify this file according to the requirements of the new application. In particular, one has to specify dependencies on other packages by modifying the field `dependencies` in the `package.json` file,<sup>2</sup> e.g.:

```
{
  ...,
  "dependencies": {
    "base": ">= 3.0.0, < 4.0.0",
    "json": "~> 3.0.0"
  }
}
```

After modifying the metadata, one can run

```
> cypm install
```

---

<sup>2</sup>One could also use the command `"cypm add -d PACKAGE"` to add new dependencies in this file.

(inside the package directory `myproject`) to resolve, download, and install all dependencies of the current package. Then one can invoke **PAKCS** and use the modules of all specified packages.

When the development of the application is completed, one can specify the name of the main module and the executable to be generated in the file `package.json` as field `executable`:

```
{
  ...,
  "executable": {
    "name": "myexec",
    "main": "Start"
  }
}
```

The name of the executable must be defined (with key `name`) whereas the name of the main module (key `main`) is optional (if it is missing, the name `Main` is taken). The main module must export a function

```
main :: IO ()
```

which starts the application. If a package contains an `executable` specification, the command

```
> cypm install
```

also compiles the main module and installs the executable in the default directory `$HOME/.cpm/bin` (see Section [5.2](#)).

**Part III**

**Design Patterns**

# Chapter 6

## Design Patterns

### 6.1 Overview

A *design pattern* is a proven solution to a recurring problem in software design and development. A typical pattern is not reusable code, as a library function would be, but consists of problems, motivations, and design decisions related to the elements of a software artifact. Many functional logic design patterns are centered on the characteristic features of the paradigm, non-determinism and logic variables.

Patterns originated for object-oriented programming languages and became an important discipline in computer science after [11]. Design patterns for functional logic programming were introduced and further developed in [5, 7]. We present a pattern using *tags*, typically a one-line description of some key element of a problem or its solution. In this tutorial, we use only four simple tags: *name*, *intent*, *solution*, and *structure* with self-explaining meaning.

#### 6.1.1 Deep selection

Name	<i>Deep selection</i>
Intent	pattern matching at arbitrary depth in recursive types
Applicability	select an element with given properties in a structure
Structure	combine a type generator with a functional pattern

Recursively defined types, such as lists and trees, have components at arbitrary depths that cannot be selected by pattern matching because pattern matching selects components only at predetermined positions. For recursively defined types, the selection of some element with a given property in a data structure typically requires code for the traversal of the structure which is intertwined with the code for using the element. The combination of functional patterns with type generators allows us to select elements arbitrarily nested in a structure in a pattern matching-like fashion without explicit traversal of the structure and mingling of different functionalities of a problem.

We show the application of this pattern in one example. Consider a simple type for representing arithmetic expressions:

```
data Exp = Lit Int
         | Var [Char]
```

```

| Add Exp Exp
| Mul Exp Exp

```

For example, the expression  $x + 1$  is encoded as  $e = \text{Add } (\text{Var } "x") (\text{Lit } 1)$ . Suppose that we want to match an expression with some property, e.g., the expression is a variable, regardless of whether it occurs. First, we define a function, *withSub*, that takes an expression  $t$  and non-deterministically generates some expression with  $t$  as subexpression.

```

withSub exp = exp
            ? op (withSub exp) unknown
            ? op unknown (withSub exp)
where op = Add ? Mul

```

For example, if  $t = \text{Var } "x"$ , then  $\text{withSub } t$  evaluates, among other possibilities, to an expression matching the expression  $e$  discussed earlier. Thus, using functional patterns, Sect. 3.5.5, we can pattern match a subexpression  $t$  anywhere in an expression  $e$ .

To see this in action, consider the function *varOf* defined below. This function takes an expression  $e$  and returns the identifier of a variable occurring anywhere in  $e$ . With ordinary pattern matching, only a variable at a fixed position, e.g., the root or the left argument of an expression, can be matched. With *withSub* we match any variable anywhere:

```

varOf :: Exp -> String
varOf (withSub (Var v)) = v

```

For example, the set of the identifiers of all the variables of occurring in an expression  $e$  is simply obtained with the set function of *varOf*, i.e.,  $\text{varOf}_S e$  [[Browse Program](#)][[Download Program](#)].

### 6.1.2 Constrained Constructor

Name	<i>Constrained Constructor</i>
Intent	prevent invoking a constructor that might create invalid data
Applicability	a type is too general for a problem
Structure	define a function that either invokes a constructor or fails

The signature of a functional logic program is partitioned into *defined operations* and *data constructors*. They differ in that operations manipulate data by means of rewrite rules, whereas constructors create data and have no associated rewrite rules. Therefore, a constructor symbol cannot perform any checks on the arguments to which it is applied. If a constructor is invoked with arguments of the correct types, but inappropriate values, conceptually invalid data is created. We use an example to clarify this point.

The *Missionaries and Cannibals* puzzle is stated as follows. Three missionaries and three cannibals want to cross a river with a boat that holds up to two people. Furthermore, the missionaries, if any, on either bank of the river cannot be outnumbered by the cannibals (otherwise, as the intuition hints, they would be eaten by the cannibals).

A state of this puzzle is represented by the number of missionaries and cannibals and the presence of the boat on an arbitrarily chosen bank of the river, by convention the *initial* one:

```
data State = State Int Int Bool
```

For example, with suitable conventions, `(State 3 3 True)` represents the initial state. The simplicity of this representation has the drawback that invalid states, e.g., those with more than 6 people, can be created as well. Unless complex and possibly inefficient types for the state are defined, it is not possible to avoid the creation of invalid states using constructors alone.

The *Constrained Constructor* pattern avoids the creation of invalid states. The programmer invokes the constructor indirectly through the following function:

```
makeState m c b | valid && safe = State m c b
  where valid = 0<=m && m<=3 \boolAnd 0<=c && c<=3
        safe  = m==3 || m==0 || m==c
```

Function `makeState` invokes the constructor only after checking that only states that are consistent with the physical conditions of the puzzle and are safe for the missionaries will be created. For example, `(State 2 1 -)` is not safe since on one bank of the river the cannibals outnumber the missionaries and therefore should not be created. In fact, the call `makeState21-` fails because the rule’s condition is not satisfied. In a suitable non-deterministic program, this failure can be simply and silently ignored.

Operation `makeState` eases the definition of an operation, say `move`, to move people and boat across the river:

```
move (State m c True)
  = makeState (m-2) c False      -- move 2 missionaries
  ? makeState (m-1) c False      -- move 1 missionary
  ? makeState m (c-2) False      -- move 2 cannibals
  ? ...
```

since “undesirable” states are never produced [\[Browse Program\]](#)[\[Download Program\]](#).

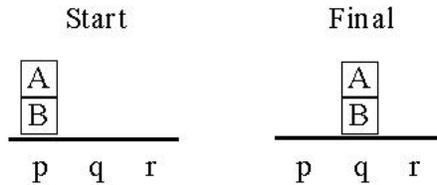
### 6.1.3 Non-determinism introduction and elimination

Name	<i>Non-determinism introduction and elimination</i>
Intent	use different algorithms for the same problem
Applicability	some algorithm is too slow or it may be incorrect
Structure	either replace non-deterministic code with deterministic one or vice versa

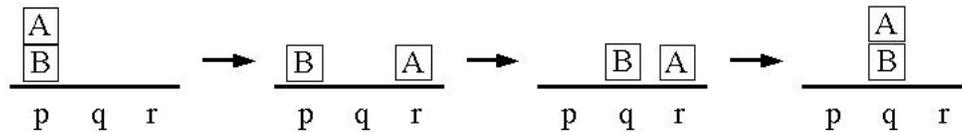
Specifications are often non-deterministic because in many cases non-determinism defines the desired results of a computation more easily than by other means. We have seen this practice in several previous examples. Thus, it is not unusual for programmers to initially code a non-deterministic prototype even for deterministic problems because this approach produces correct programs quickly.

In some cases, a non-deterministic program is not efficient enough to solve a problem of interesting size. Reducing the non-determinism of the program, e.g., by taking advantage of domain knowledge, may improve the efficiency of execution. Below, is an example. The “*blocks world*” [\[24\]](#) consists of 3 possibly empty piles, labeled *p*, *q* and *r*, of unique blocks

labeled **A**, **B**, **C**, etc. “*Start*” and “*Final*” below are two examples of blocks worlds from [10].



A blocks world “*problem*” consists of two worlds, like *Start* and *Final* above. Its solution consists in the moves that produce the second world from the first one. A “*move*” transfers the block on top of a pile to the top of another pile. No other blocks are affected by the move. Below is an example of a solution from *Start* to *Final*.



In our prototype, blocks are encoded as an enumerated type. A world is three stacks of blocks. A solution is a sequence of worlds. A problem is a pair of words.

```

data Block = A | B | C | D | E deriving Eq
type Stack = [Block]
type World = (Stack, Stack, Stack)
type Trace = [World]
data Problem = Problem World World

simpleProblem, difficultProblem :: Problem
simpleProblem = Problem ([A,B], [], []) ([], [A,B], [])
difficultProblem = Problem ([A,B,C,D,E], [], []) ([], [C,B,A,D,E], [])

```

We define two functions to solve a blocks world problem. Function `move` moves the block at the top of a pile to the top of another different pile. Both the origin and the destination pile of a move are non-deterministically selected. Function `extend` takes a sequence of blocks world states, that we call a *trace*, that when reversed satisfies the following invariant: (1) the first block is the start state, (2) any other block is obtained from the previous one by a move, and (3) no element, with the possible exception of the last one, is repeated.

Function `extend` performs the following tests and corresponding actions on the last element, *t*, of the trace (the first element actually, since the trace is reversed): (1) if *t* is the final world, the trace is a solution, (2) if *t* is repeated in the trace, the computation is aborted, otherwise (3) the trace is extended with a move from *t*:

```

move :: World -> World
move (x:xs, ys, zs) = (xs, x:ys, zs) ? (xs, ys, x:zs) -- p -> q/r
move (xs, y:ys, zs) = (y:xs, ys, zs) ? (xs, ys, y:zs) -- q -> p/r

```

```

move (xs, ys, z:zs) = (z:xs, ys, zs) ? (xs, z:ys, zs) -- r -> p/q

extend :: Trace -> World -> Trace
extend trace@(t:ts) goal
  | t == goal      = reverse trace
  | t 'elem' ts    = failed
  | otherwise      = extend (move t : trace) goal

main :: Problem -> Trace
main = extend [s] f where Problem s f = simpleProblem

```

The **PAKCS** interpreter produces 40 solutions of `simpleProblem` in which the number of moves ranges from 3 to 10, in a fraction of a second. However, it does not produce any solution of `difficultProblem` in over an hour. We are guessing that the reason is that the non-determinism of `move` is too “unfocused.” [[Browse Program](#)][[Download Program](#)].

We reduce the non-determinism of the previous program using two strategies. We favor moves that put a block in its final place and by we avoid moves that take a block away from its final place. Function `moveToGoal` is quite similar to function `move` of the previous program, but it moves a block only if the block ends up into its final place. If such a move is not available, the move is computed by function `noMoveFromGoal`. This function is again quite similar to `move`, but a block that is already in its final place is never moved.

Observe that `noMoveFromGoal` would fail if called on the final state of a blocks world problem. An invariant of this and the previous program is that no move is attempted on any final state.

```

moveToGoal :: World -> World -> World
moveToGoal (x:xs, ys, zs) (_, _++x:ys, _) = (xs, x:ys, zs) -- p -> q
moveToGoal (x:xs, ys, zs) (_, _, _++x:zs) = (xs, ys, x:zs) -- p -> r
moveToGoal (xs, y:ys, zs) (_++y:xs, _, _) = (y:xs, ys, zs) -- q -> p
moveToGoal (xs, y:ys, zs) (_, _, _++y:zs) = (xs, ys, y:zs) -- q -> r
moveToGoal (xs, ys, z:zs) (_++z:xs, _, _) = (z:xs, ys, zs) -- r -> q
moveToGoal (xs, ys, z:zs) (_, _++z:ys, _) = (xs, z:ys, zs) -- r -> p
moveToGoal'default w g = noMoveFromGoal w g

noMoveFromGoal :: World -> World -> World
noMoveFromGoal (x:xs, ys, zs) (g, _, _)
  | not (isSuffixOf (x:xs) g) = (xs, x:ys, zs) ? (xs, ys, x:zs)
noMoveFromGoal (xs, y:ys, zs) (_, g, _)
  | not (isSuffixOf (y:ys) g) = (y:xs, ys, zs) ? (xs, ys, y:zs)
noMoveFromGoal (xs, ys, z:zs) (_, _, g)
  | not (isSuffixOf (z:zs) g) = (z:xs, ys, zs) ? (xs, z:ys, zs)

extend :: Trace -> World -> Trace
extend trace@(t:ts) goal
  | t == goal      = reverse trace
  | t 'elem' ts    = failed
  | otherwise      = extend (moveToGoal t goal : trace) goal

```

```
main :: Trace
main = selectValue (set2 extend [s] f)
  where Problem s f= difficultProblem
```

The **PAKCS** interpreter produces 6 solutions of `simpleProblem` in which the number of moves ranges from 3 to 7, in a fraction of a second. It also produces a solution of `difficultProblem` in a few seconds, but this solution is 170 moves long. There exists a solution of this problem which is only 12 moves long. [\[Browse Program\]](#)[\[Download Program\]](#).

The previous example and discussion shows that reducing the non-determinism of a program may increase its efficiency. Often, it also increases its complexity. This pattern comes in a dual form. In some situations, e.g., if a program is producing unexpected results, it may be useful to increase the program non-determinism. This change will likely decrease the program efficiency, but increase its simplicity. With a simpler program it may be easier to assess or verify whether a result of a computation is expected.

## Part IV

# Applications & Libraries

# Chapter 7

## Web Programming

### 7.1 Overview

Due to the ubiquity of the world wide web (WWW or “web” for short), many applications offer web-based interfaces in order to support convenient access to them. This chapter describes how one can implement web-based interfaces in Curry. We will see that the functional and logic programming features of Curry are quite useful in providing a high-level programming interface for such applications so that Curry can also be used as a language for “web scripting,” i.e., for writing web interfaces in a concise manner.

This chapter requires some basic knowledge about the structure of HTML, the “Hypertext Markup Language” for describing the general form and layout of documents presented by web browsers. Up-to-date information about HTML is available from the World Wide Web Consortium ([W3C](http://www.w3.org/)).

The approach to web programming described in this chapter is based on the package `html2`.<sup>1</sup> It is based on the library HTML contained in earlier versions of `PAKCS` described in [16]. Ideas and details about this newer library for web programming can also be found in [19].

### 7.2 Representing HTML Documents in Curry

HTML is a language for specifying the structure and layout of web documents. We also say “HTML document” for a text written in the syntax of HTML. Basically, an HTML document consists of the following elements:

- elementary text
- *tags* with other HTML elements as contents, like headers (`h1`, `h2`,...), lists (`ul`, `ol`,...), etc.
- tags without contents, like line breaks (`br`), images (`img`), etc.

The plain syntax of HTML, which is interpreted by a web browser when displaying HTML documents, requires tags be enclosed in pointed brackets (`<...>`). The contents of a tag is

---

<sup>1</sup><https://cpm.curry-lang.org/pkgs/html2.html>

written between an opening and a closing tag where the closing tag has the same name as the opening tag but is preceded by a slash. Tags can also contain *attributes* to attach specific information to tags. If present, attributes are written in the form “*name=value*” after the opening tag’s name and before its right bracket.

For instance, “i” and “b” are tags to specify that their contents should be set using an italic and bold font, respectively. Thus, the HTML text

```
This is the <i>italic</i> and the <b>bold</b> font.
```

would be displayed by a web browser as this:

This is the *italic* and the **bold** font.

Tags without contents have no closing tag. An example is the tag for including images in web documents, where the attribute “src” specifies the file containing the picture and “alt” specifies a text to be displayed as an alternative to the picture:

```

```

A program with a web interface must generate HTML documents that are displayed in the client’s browser. In principle, we can do this in Curry by printing the text of the HTML document directly, as in:

```
writeHTML = do
  putStrLn "This is the "
  putStrLn "<i>italic</i> and the "
  putStrLn "<b>bold</b> font."
```

If the program becomes more complex and generates the HTML text by various functions, there is the risk that the generated HTML text is syntactically not correct. For instance, the tags with contents must be properly nested, i.e., the following text is not valid in HTML (although browser can display it but may become confused by illegal HTML documents):

```
This is <b>bold and also <i>italic</b></i>.
```

To avoid such problems in applications programs, one can introduce an *abstraction layer* where HTML documents are modeled as terms of a specific datatype. Thus, a web application program generates such abstract HTML documents instead of the concrete HTML text. This has the advantage that ill-formed web documents correspond to ill-formed expressions in Curry which would immediately be rejected by the compiler. The actual printing of the concrete HTML text is done by a wrapper function that translates an abstract HTML document into a string.

For representing abstract HTML documents in Curry, we define the following datatype of *basic HTML expressions*:

```
data BaseHtml = BaseText String
              | BaseStruct String Attrs [BaseHtml]

type Attrs = [(String ,String)
```

The constructor `BaseText` corresponds to elementary text in an HTML document, whereas the constructor `BaseStruct` correspond to HTML elements with a tag and attributes. Thus, the parameter of type “`Attrs`”, which is a type synonym for “`[(String,String)]`”, is the list of attributes, i.e., name/value pairs.

For instance, our first HTML document above is represented with this datatype as the following list of HTML expressions:

```
[BaseText "This is the ",
 BaseStruct "i" [] [BaseText "italic"],
 BaseText " and the ",
 BaseStruct "b" [] [BaseText "bold"],
 BaseText " font."]
```

Similarly, the image tag above is represented as follows:

```
BaseStruct "img" [("src","picture.jpg"),("alt","Picture")] []
```

Obviously, we can specify any HTML document in this form but this becomes very tedious for a programmer. To avoid this, we define several functions as useful abbreviations of common HTML tags:

```
h1      hexps = BaseStruct "h1" [] hexps           -- header 1
h2      hexps = BaseStruct "h2" [] hexps           -- header 2
...
bold    hexps = BaseStruct "b"  [] hexps           -- bold font
italic  hexps = BaseStruct "i"  [] hexps           -- italic font
hrule   = BaseStruct "hr"  [] []                   -- horizontal rule
breakline = BaseStruct "br"  [] []                   -- line break
image src alt = BaseStruct "img" [("src",src),("alt",alt)] [] -- image
...
```

Characters that have a special meaning in HTML, like “`<`”, “`>`”, “`&`”, “`”`”, should be quoted in elementary HTML texts to avoid ill-formed HTML documents. Thus, we define a function “`htxt`” for writing strings as elementary HTML texts where the special characters are quoted by the function “`htmlQuote`”:

```
htxt    :: String -> BaseHtml
htxt s = BaseText (htmlQuote s)

htmlQuote :: String -> String
htmlQuote [] = []
htmlQuote (c:cs) | c=='<'  = "&lt;"  ++ htmlQuote cs
                  | c=='>'  = "&gt;"  ++ htmlQuote cs
                  | c=='&'  = "&amp;" ++ htmlQuote cs
                  | c=='"'  = "&quot;" ++ htmlQuote cs
                  | otherwise = c : htmlQuote cs
```

Now we can represent our first HTML document above as follows:

```
[htxt "This is the ", italic [htxt "italic"],
```

```
htxt " and the ", bold [htxt "bold"], htxt " font."]
```

All the definitions we have introduced so far are contained in the library “HTML.Base” of the Curry package `html2`. In order to use this library, one has to add it as a dependency by the `CPM` command (see Section 5.1)

```
> cypm add html2
```

and add the import declaration

```
import HTML.Base
```

in the header of the Curry program. The library `HTML.Base` also defines a wrapper function `showBaseHtmls` to generate the concrete textual representation of an abstract HTML expression. For instance, the value of

```
showBaseHtmls [h1 [htxt "Hello World"], italic [htxt "Hello"], htxt " world!"]
```

is the string

```
<h1>
  Hello World
</h1>
<i>Hello</i>
world!
```

In order to generate a complete HTML page with header information, the library `HTML.Base` contains the following definition of HTML pages:

```
data HtmlPage = HtmlPage String [PageParam] [BaseHtml]
```

The first argument is the title of the page and the third argument is the contents of the page. The second argument is a list of optional parameters, like encoding scheme, style sheets etc. Since they are seldom used in standard pages, the library `HTML.Base` contains also the following function to specify HTML pages without optional parameters:

```
page :: String -> [BaseHtml] -> Htmlpage
page title hexps = HtmlPage title [] hexps
```

Furthermore, the library `HTML.Base` defines a wrapper function

```
showHtmlPage :: HtmlPage -> String
```

to generate the concrete textual representation of a complete HTML page with head and body parts. For instance, the value of

```
showHtmlPage (page "Hello" [h1 [htxt "Hello World"],
                             italic [htxt "Hello"], htxt " world!"])
```

is the string

```
<!DOCTYPE html>
```

```

<html lang="en">
  <head>
    <title>
      Hello
    </title>
    <meta http-equiv="Content-Type" content="text/html; charset=utf-8"/>
  </head>

  <body>
    <h1>
      Hello World
    </h1>
    <i>Hello</i>
    world!
  </body>
</html>

```

We can use these functions to write Curry programs that generate HTML documents. For instance, consider the generation of an HTML document that contains a list of all multiplications of digits, i.e., a line in this document should look as follows:

The product of **7** and **6** is **42**

First, we define a list of all triples containing such multiplications by the use of list comprehensions (compare Section 4.2.4):

```

multiplications = [ (x,y,x*y) | x <- [1..10], y <- [1..x] ]

```

Each triple is translated into a list of HTML expressions specifying the layout of a line:

```

mult2html :: (Int,Int,Int) -> [BaseHtml]
mult2html (x,y,z) =
  [htxt "The product of ", bold [htxt (show x)],
   htxt " and ", bold [htxt (show y)],
   htxt " is ", bold [htxt (show z)], breakline]

```

Now can use these definitions to define the complete HTML document (the prelude function `concatMap` applies a function that maps elements to lists to each element of a list and concatenates the result into a single list) [[Browse Program](#)][[Download Program](#)]:

```

htmlMultiplications =
  [h1 [htxt "Multiplication of Digits"]] ++ concatMap mult2html multiplications

```

For instance, we can use the latter function to store the HTML page in a file named “multtable.html” by evaluating the expression:

```

writeFile "multtable.html"
  (showHtmlPage (page "Multiplication" htmlMultiplications))

```

**Exercise 14** Define a function `boldItalic` to translate text files into HTML documents. The function has two arguments: the name of the input text file and the name of the file

where the HTML page should be stored. The HTML document should have the same line structure as the input but the lines should be formatted in bold and italic, i.e, first line in bold, second in italic, third in bold, fourth in italic, etc. Hint: use the prelude function `lines` to split a string into a list of lines. [\[Browse Answer\]](#)[\[Download Answer\]](#)

## 7.3 Server-Side Web Scripts

We have seen so far how to write programs that create static HTML documents. Such programs could be useful to transform existing data into a static set of HTML pages. In contrast, the contents of *dynamic web pages* is computed at the time they are requested by a client (usually, a web browser). Technically, the creation of dynamic web pages is supported by web servers by so-called CGI (Common Gateway Interface) programs. If a web server is asked for a document with the suffix “.cgi” instead of “.html” (the exact behavior is defined in the configuration of the web server; see also Section 7.4 below), then the server does not return the contents of the corresponding file but executes the file (the “CGI program”) and returns the standard output produced by this program. Thus, a CGI program must write an HTML document on its standard output. The CGI program can also take user input in an HTML form into account; this is described in Section 7.5.

Since the CGI program is some executable stored on the web server, it can be written in any programming language. Thus, we can also write a Curry program which generates prints an HTML document when it is executed. As already discussed above, writing raw HTML documents could be error prone so that it is better create HTML data structures. Therefore, the library `HTML.Base` supports the creation of dynamic web pages by compiling a Curry program with a main operation of type

```
main :: IO HtmlPage
```

into an executable which prints the corresponding HTML document (the actual application of this compiler is described in the next section). Since this is an I/O operation, the contents of the generated HTML documents could also depend on the environment of the web server, e.g., information stored in the file system or databases.

As a first example, we want to generate a CGI program that computes the above multiplications of digits on demand. For this purpose, we define the following operation `multPage` (the right-associate operator “\$” is defined with a low precedence in the prelude and denotes function application; it is often used to avoid brackets, e.g., the expression “f \$ g \$ 3+4” is equivalent to “f (g (3+4))”) [\[Browse Program\]](#)[\[Download Program\]](#):

```
multPage :: IO HtmlPage
multPage =
  return $ headerPage "Multiplication of Digits" htmlMultiplications
```

Here we use the operation `headerPage` which is similar to `page` but adds the page title as a header line:

```
headerPage :: String -> [BaseHtml] -> HtmlPage
headerPage title hexps = page title (h1 [htxt title] : hexps)
```

To see an application of accessing the server environment, we define a form that shows the current date and time of the server (the IO action `getLocalTime`, defined in the standard library `Data.Time` contained in Curry package `time`, returns the local date and time in some internal representation which can be converted into a readable string by the function `calendarTimeToString`) [[Browse Program](#)][[Download Program](#)]:

```
timePage :: IO HtmlPage
timePage = do
  time <- getLocalTime
  return $ page "Current Server Time"
    [h1 [htxt $ "Current date and time: " ++ calendarTimeToString time]]
```

The installation of such web programs on a web server is described in the following section.

## 7.4 Installing Web Programs

Although the installation of CGI programs highly depends on the web server, this section provides some hints so that you can execute the programs described in this chapter on your web server. Clearly, your web server must be configured to enable the execution of CGI programs. Fortunately, most web servers support CGI programs, though they will likely require special configuring by the system administrator. A web server can be configured to interpret any file ending with “.cgi” and execute it when requested, or it can be also configured to execute only CGI programs stored in a particular directory, e.g., “cgi-bin”. Ask your system administrator for the instructions on CGI execution that are specific to your system.

In order to execute any web program written with the library `HTML.Base`, the Curry-to-CGI compiler `curry2cgi` is required. It can easily be installed by executing the following CPM command (see also Section 5.2) on the web server (where `PAKCS` should be already installed):

```
> cypm install html2
```

Now the installation of a CGI program is quite simple. Assume you have written a Curry program “myscript.curry” containing a definition of a form function “main” of type “IO HtmlPage” (see previous section). Then you can compile it into an executable CGI program by the command

```
> curry2cgi myscript
```

This creates (after successful compilation) an executable program “myscript.cgi”. If your main form function has a name different from the default `main`, you can specify it with option “-m”. For instance, the command

```
> curry2cgi -m myForm myscript
```

creates a CGI program with form function “myForm”. In general, the parameter following “-m” can be any Curry expression of type “IO HtmlPage”.<sup>2</sup>

---

<sup>2</sup>Since this expression is executed as the main program, all symbols of this expression must be exported from the Curry program.

Similarly, the option “-o” can be used to install the CGI program under a different name. For instance, the command

```
> curry2cgi -o ~/cgi-bin/myscript.cgi -m myForm myscript
```

installs the executable CGI program in the file “~/cgi-bin/myscript.cgi”. Depending on the configuration of your web server, you can execute the CGI program by requesting the document with a URL like “http://your.server.name/cgi-bin/myscript.cgi” in your web browser.

## 7.5 Forms with User Input

In many applications, dynamic web pages should not only depend on the environment of the web server but also on the input provided by the client (i.e., the user contacting the server via its browser). In principle, this is possible since HTML includes also elements for user input (text fields, buttons, etc) which is sent to the web server when requesting a document. How can we access the user input in a CGI program running on the server? The whole purpose of the Common Gateway Interface is to define a method to send information to the server and from the web browser, hence the name Common Gateway. Fortunately, it is not necessary to know all the details of CGI since the library `HTML.Base` defines an abstraction layer to provide a comfortable access to user inputs. This abstraction layer exploits the functional and logic features of Curry and will be explained in this section.

Input elements are contained in *HTML forms* that are embedded in HTML pages. If a form is submitted to the web server, the contents of the input elements, e.g., the text typed into text fields, is transmitted to the web server. To refer to the contents of input elements, there is a type

```
data HtmlRef = ...
```

This type is abstract and the library `HTML.Base` does not export any constructor for this type. We will see later how to use such abstract *HTML references*.

The library `HTML.Base` uses such references in the definitions of the various input elements occurring in HTML forms. For instance, the element “`textField`” defines an HTML input element where the user can type a line of text:

```
textField :: HtmlRef -> String -> HtmlExp
```

The first argument is the reference to this input field and the second argument is the initial contents shown in the field. It should be noted that this input element has type `HtmlExp` rather than `BaseHtml`. This distinction is useful to avoid errors with input fields. Since input fields can only occur inside forms, forms contain data of type `HtmlExp` and are embedded in HTML pages, i.e., data of type `BaseHtml`. Note that the abbreviations of common HTML tags shown above (`htxt`, `h1`, `h2`, *italic*, ...) are actually overloaded (via type classes) so that they can be used as `BaseHtml` and also as `HtmlExp` data.

How can we use a `textField` if there are no constructors of type `HtmlRef`? The simple and may be surprising answer is: by logic variables! For instance, a form containing a string and an input field can be defined as follows:

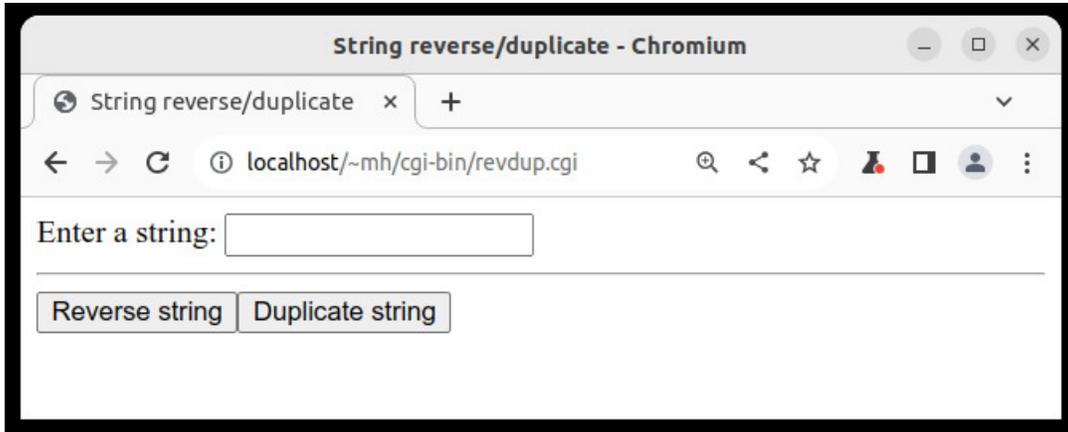


Figure 7.1: A simple string reverse/duplication form

```
rdForm = [htxt "Enter a string: ", textField tref ""]
  where tref free
```

A `HtmlRef` variable serves as a reference to the corresponding input field to access the user's input. Raw CGI requires concrete strings as references (attribute “name” of “input” tags) which is error-prone (since typos in these strings lead to run-time errors). However, the concrete strings are not important, and so the logic variables are sufficient. It is only important to use them when computing the answer to the client. For this purpose, the library `HTML.Base` defines an *HTML environment* as a mapping from HTML references to strings:

```
type HtmlEnv = HtmlRef -> String
```

An HTML environment is used to collect the input of the user when computing the response. The computation of the response is done by an HTML *event handler* that is attached to each button for submitting a form to the web server. For this purpose, the library `HTML.Base` defines the type of HTML event handlers as

```
type HtmlHandler = HtmlEnv -> IO HtmlPage
```

i.e., an event handler is called with the current HTML environment and yields an I/O action that returns a new HTML page to be sent back to the client. Thus, the library `HTML.Base` contains the following type definition for a button to submit forms:

```
button :: String -> HtmlHandler -> HtmlExp
```

The first argument is the text shown on the button and the second argument is the event handler called when the user clicks this submit button.

The actual event handlers can simply be defined as local functions attached to forms so that the `HtmlRef` variables are in scope and need not be passed. To see a simple example, we show the specification of a form where the user can enter a string and choose between two actions (reverse or duplicate the string) by two submit buttons (see Figure 7.1) [[Browse Program](#)][[Download Program](#)]:

```

rdFormContents :: [HtmlExp]
rdFormContents =
  [htxt "Enter a string: ", textField tref "", hrule,
    button "Reverse string" revhandler,
    button "Duplicate string" duphandler]
where
  tref free

  revhandler env = return $ page "Answer"
    [h1 [htxt $ "Reversed input: " ++ reverse (env tref)]]

  duphandler env = return $ page "Answer"
    [h1 [htxt $ "Duplicated input: " ++ env tref ++ env tref]]

```

Note the simplicity of retrieving values entered into the form: since the event handlers are called with the appropriate environment containing these values (parameter “`env`”), they can easily access these values by applying the environment to the appropriate HTML reference, like “`(env tref)`”.

So far we have the definition of a form, but how can such forms be embedded in an HTML page? Note that a form has two different purposes:

1. A form defines the layout and input fields shown to the user.
2. A form defines the reaction via handlers when it is submitted.

For this purpose, the library `HTML.Base` distinguishes between a *form definition* and its actual *use*. For this purpose, forms must be defined as top-level entities (which will be compiled by `curry2cgi`). For this purpose, there is a constructor `simpleFormDef` (other constructors are shown later):

```
simpleFormDef :: [HtmlExp] -> HtmlFormDef ()
```

This operation wraps a form layout, possibly containing input elements and event handlers, into a form definition (the type argument of `HtmlFormDef` will be discussed later). For instance, we turn our form above into a form definition by

```
rdFormDef :: HtmlFormDef ()
rdFormDef = simpleFormDef rdFormContents
```

A defined form can be embedded into an HTML page by wrapping the form definition with operation

```
formElem :: HtmlFormDef a -> BaseHtml
```

Hence, the following code defines an HTML page containing our form:

```
rdPage :: IO HtmlPage
rdPage = return $ page "String reverse/duplicate" [formElem rdFormDef]
```

By defining the form together with the various handlers in one top-level entity, forms are more reliable compared to a separate definition of HTML structures and scripts to process

them. The advantage of distinguishing a form definition from its actual use is that we can use a form in any HTML document, in particular, recursively in the answer computed by an event handler. For instance, a form to compute the length of an input string and showing the form again in the answer can be defined as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
lengthForm = simpleFormDef
  [htxt "Enter a string: ", textField ref "", button "Length"
    (\env -> return $ page "Answer"
      [h1 [htxt $ "Length: " ++ show (length (env ref))],
        hrule, formElem lengthForm])]
  where ref free

main :: IO HtmlPage
main = return $ headerPage "String length" [formElem lengthForm]
```

## 7.6 Stateful Forms

The simple HTML forms presented so far are quite limited. Form definitions are top-level entities so that their layout is fixed, i.e., they cannot show data from a possible usage context, e.g., database entities or authentication data. In order to make forms more flexible, it should be possible that forms access some state to be shown in the form. Such *stateful forms* need only to read data, since the manipulation of data, e.g., updating a data base depending on the user input, is usually performed by the event handlers (therefore, event handlers are of type IO).

To support stateful forms, the library `HTML.Base` defines a monad `FormReader` with operations to read data (see below), i.e., the `FormReader` monad is a restriction of the `IO` monad where only read operations are supported.<sup>3</sup> Thus, a stateful form consists of a `FormReader` action to read data of some type `a` and an operation which maps values of this type into an HTML form. The library `HTML.Base` supports the definition of stateful forms by the form constructor operation

```
formDef :: FormReader a -> (a -> [HtmlExp]) -> HtmlFormDef a
```

Therefore, an operation of type `HtmlFormDef a` specifies a form which reads some data of type `a` and use this data to generate the actual HTML form.

In order to define a stateful form, we need an operation of type `FormReader a`. A difficulty in web programming is the fact that HTTP is a stateless protocol, i.e., each web page can be shown several times and there are no connections between different web pages to pass some state from one page to another. This problem is solved in typical web applications by a session concept where each user has its own session where session-local data can be stored, like the login name of a user or the contents of a virtual shopping basket. A session concept

---

<sup>3</sup>The restriction to read operations is necessary since forms might be executed several times, e.g., to construct the form layout, to start an event handler, or if the form has multiple occurrences in a web page. Thus, a form should not change the environment. Changes are only performed by the activation of some event handler.

can be implemented via cookies to identify the client in a session. To hide the details of session handling, the package `html2` contains the library `HTML.Session` which provides the following operations (the type variable `a` denotes the type of session data):

```
getSessionData    :: (Read a, Show a) => SessionStore a -> a -> FormReader a
putSessionData    :: (Read a, Show a) => SessionStore a -> a -> IO ()
removeSessionData :: (Read a, Show a) => SessionStore a -> IO ()
```

The type variable `a` specifies the type of session data. The class constraints `Read` and `Show` are required since the data is stored on the web server. “`SessionStore a`” is the type of a top-level entity referring to some memory cell containing session information of type `a`. `getSessionData` retrieves information of the current session (and returns the second argument if there is no information, e.g., in case of a new session), `putSessionData` stores information in the current session, and `removeSessionData` removes such information. A session store containing data of type `a` can be defined in a Curry program as a top-level entity by using the constructor operation

```
sessionStore :: (Read a, Show a) => String -> SessionStore a
```

The argument is a unique name (consisting of letters and digits) for the session store in the web application.<sup>4</sup>

In order to see an application of this concept, we implement a simple number guessing game: the client has to guess a number known by the server (here: 42), and for each number entered by the client the server responds whether this number is correct, smaller or larger than the number to be guessed. If the guess is not right, the answer form contains an input field where the client can enter the next guess. Moreover, the number of guesses should also be counted and shown at the end. Hence, the session state contains the number of trials and is defined as

```
trials :: SessionStore Int
trials = sessionStore "trials"
```

The form definition consists of an action that reads the current session data and the HTML form for this data [[Browse Program](#)][[Download Program](#)]:

```
guessForm :: HtmlFormDef Int
guessForm = formDef (getSessionData trials 1) guessFormHtml

guessFormHtml :: Int -> [HtmlExp]
guessFormHtml t =
  [htxt "Guess a number: ", textField nref "",
   button "Check" guessHandler]
  where
    nref free

    guessHandler env = do
```

---

<sup>4</sup>Session stores are implemented as persistent global entities, see Curry package `global`, which are stored in the file system of the server.

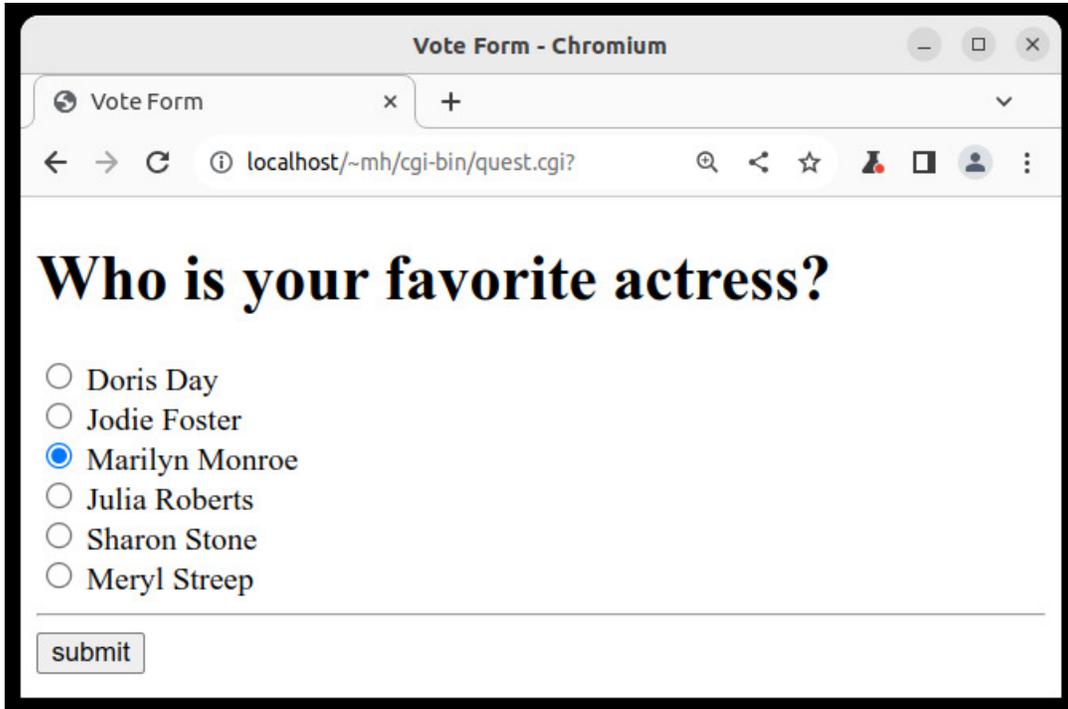


Figure 7.2: A web questionnaire

```

let n = read (env nref)
if n==42
  then do
    removeSessionData trials
    return $ headerPage ("Correct! " ++ show t ++ " guesses!") []
  else do
    putSessionData trials (t+1)
    return $ headerPage ("Too " ++ if n<42 then "small!" else "large!")
      [formElem guessForm ]

```

The form handler reads the user input from the HTML environment (one could add an additional check whether the input is a number string) and compares it with the “secret” number. If it is equal, the session data is removed before returning the answer, otherwise the session data is updated so that the next form invocation gets the updated data.

## 7.7 Example: A Web Questionnaire

In many web applications, clients want to store or update information on the server, e.g., by putting orders for books, flight tickets, etc. In this section we show an example where a client can change persistent data stored on the web server.

Consider the implementation of a web-based questionnaire which allows the clients to vote on a particular topic. Figure 7.2 shows an example of such a questionnaire. The votes are stored on the web server. The current votings are shown after a client submits a vote (see Figure 7.3).

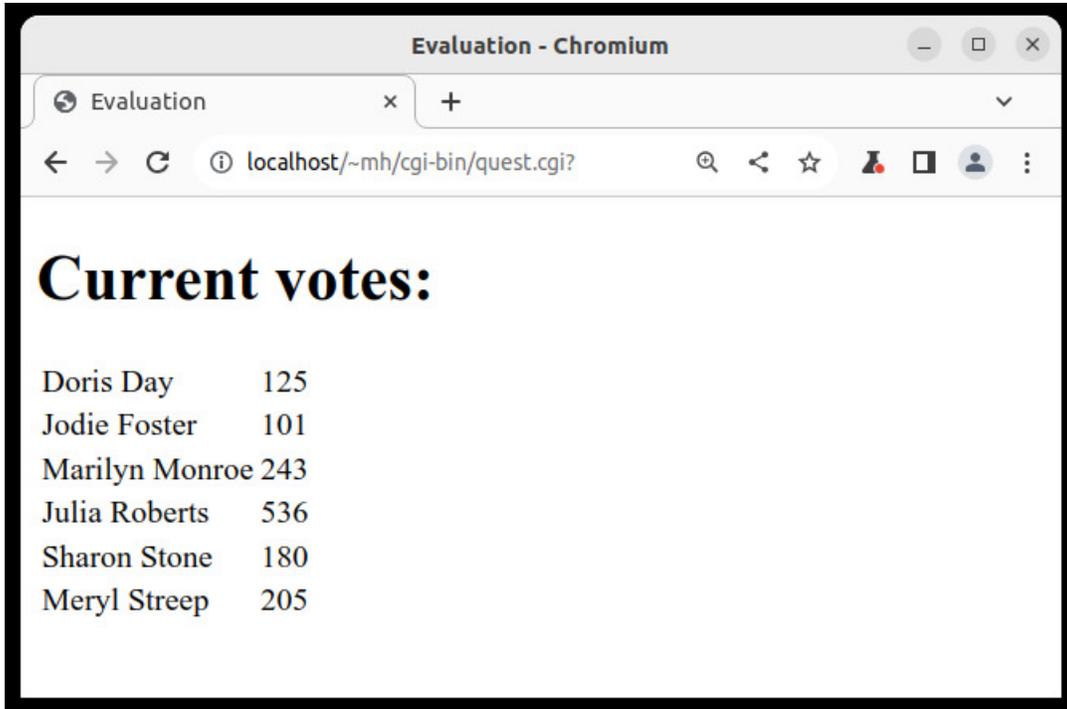


Figure 7.3: Answer to the web questionnaire

In order to provide an implementation that is easy to maintain, we define the main question and the choices for the answers as constants in our program so that they can be easily adapted to other questionnaires:

```
question :: String
question = "Who is your favorite actress?"

choices :: [String]
choices = ["Doris Day", "Jodie Foster", "Marilyn Monroe",
          "Julia Roberts", "Sharon Stone", "Meryl Streep"]
```

The current votes are stored in a file on the web server. We define the name of this file as a constant in our program:

```
voteFile :: String
voteFile = "votes.data"
```

For the sake of simplicity, this file is a simple text file. If there are  $n$  choices for voting, the file has  $n$  lines where each line contains the textual representation of the number of votes for the corresponding choice. Thus, the following operation reads the vote file and returns the list of numbers in this file or, if the file does not exist, initializes the vote file and returns zeros (the prelude function `lines` breaks a string into a list of lines, where lines are separated by newline characters, and the opposite function `unlines` concatenates a list of strings into lines).

```
readVoteFile :: IO [Int]
```

```

readVoteFile = do
  existnumfile <- doesFileExist voteFile
  if existnumfile
    then do vfcont <- readFile voteFile
             return (map read (lines vfcont))
    else do let nums = take (length choices) (repeat 0)
             writeFile voteFile (unlines (map show nums))
             return nums

```

To update the vote file, we define `overwriteVoteFile` that writes a list of numbers into the vote file. The numbers are written into a new file that is moved to the vote file in order to avoid an overlapping between reading and writing the same file. `doesFileExist`, `removeFile`, and `renameFile` are I/O operations defined in the library `System.Directory` (from package `directory`) to check the existence of a file, delete a file, and rename a file, respectively.

```

overwriteVoteFile :: [Int] -> IO ()
overwriteVoteFile nums = do
  writeFile (voteFile ++ ".new") (unlines (map show nums))
  removeFile voteFile
  renameFile (voteFile ++ ".new") voteFile

```

When a client submits a vote, we have to increment the corresponding number in the vote file. This can be easily done by reading the current votes and writing the votes that are incremented by the auxiliary function `incNth`:

```

incNumberInFile :: Int -> IO ()
incNumberInFile voteindex = do
  nums <- readVoteFile
  overwriteVoteFile (incNth nums voteindex)
  where
    incNth [] _ = []
    incNth (x:xs) n | n==0 = (x+1) : xs
                    | otherwise = x : incNth xs (n-1)

```

Now we have all auxiliary definitions that are necessary to define the web script. First, we show the definition of the HTML page “`evalPage`” that shows the current votes (which produces the result shown in Figure 7.3). The prelude function “`zip`” joins two lists into one list of pairs of corresponding elements.

```

evalPage :: IO HtmlPage
evalPage = do
  votes <- exclusiveIO (voteFile ++ ".lock") readVoteFile
  return $ form "Evaluation"
    [h1 [htxt "Current votes:"],
     table (map (\(s,v) -> [[htxt s], [htxt $ show v]])
            (zip choices votes))]

```

Note that we ensure the exclusive access to the vote file by the use of the operation

`exclusiveIO`.<sup>5</sup> This is necessary since there is not much control on the access to web pages by clients. In particular, the same CGI program might be executed in parallel if two clients accessing them simultaneously. This can cause problems if both read and update the same information. Thus, it is mandatory to ensure exclusive data access in web applications which might change data. If the data is stored in files, it must be manually done, as above. If the data is stored in databases, the database system ensures the exclusive access but one has to take care on the definition of transactions.

Now we can define our form that allows the user to submit a vote (see Figure 7.2). It uses radio buttons as input elements. Radio buttons are lists of buttons where exactly one button can be turned on. Thus, all buttons have the same HTML reference but different values. When a form is submitted, the HTML environment maps the HTML reference to the value of the selected radio button. A complete radio button suite consists always of a main button (`radioMain`) which is initially on and some further buttons with the same HTML reference as the main button (`radioOthers`) that are initially off. In our example, we associate to each button the index of the corresponding choice as a value. The event handler `questHandler` increments the appropriate vote number and returns the current votes by the use of `evalPage` [[Browse Program](#)][[Download Program](#)]:

```
questForm :: HtmlFormDef ()
questForm = simpleFormDef $
  [h1 [htxt question],
   radioMain vref "0", htxt (head choices), breakline] ++
  concatMap (\(i,s) -> [radioOther vref (show i), htxt s, breakline])
            (zip [1..] (tail choices)) ++
  [hrule, button "submit" questHandler]
where
  vref free

  questHandler env = do
    exclusiveIO (voteFile ++ ".lock")
                (incNumberInFile (read (env vref)))
    evalPage

main :: IO HtmlPage
main = return $ page "Vote Form" [formElem questForm]
```

## 7.8 Finding Bugs

Since debugging of CGI programs can be quite tedious, here are some hints on how to debug CGI programs.

If the execution of the CGI program produces some run-time error (e.g., access to a non-existing files), the error message should be shown in the web page. Furthermore, messages written to standard error output are collected in the log file of the web script. For instance, if the web script is stored at location `cgi-bin/myscript.cgi`, the log file is

---

<sup>5</sup>The operation `exclusiveIO` is defined in the library `System.IOExts` contained in the package `io-extra`.

`cgi-bin/myscript.cgi.log`. Hence, if you want to put some debug output in your web script, you should write it to standard error, e.g.,

```
hPutStrLn stderr "A log message"
```

(where `hPutStrLn` and `stderr` are defined in the standard library `IO`).

The use of logic variables as references to input elements in HTML forms ensures that typos in the name of references can be detected by the compiler (e.g., resulting in an “undeclared identifier” error message), in contrast to traditional approaches to CGI programming using plain strings as references. However, if we use the same logic variable for two different input elements, this is not detected by the compiler (which is not worse than traditional approaches where this is also not detected) but results in a run-time error that is not easy to understand due to the implementation of the library `HTML.Base` in Curry. In this case, the web script might fail with a message like “No value found”. Thus, you should check your source program for these possible errors or add some debug output, as described above, to your script.

## 7.9 Advanced Web Programming

This section discusses some further features which are useful for writing web applications in Curry. *URL parameters* can be exploited to write generic web scripts. *Cookies* are useful to store information about the client between different web scripts. *Style sheets* can be used to modify and add new presentation styles for web documents.

### 7.9.1 URL Parameters

In some situations it is preferable to have generic web scripts that can be applied in various situations described by parameters. For instance, if we want to write a web application that allows the navigation through a hierarchical structure, one does not want to write a different script for each different level of the structure but it is preferable to write a single script that can be applied to different points in the structure. This is possible by attaching a parameter (a string) to the URL of a script. For instance, a URL can have the form “`http://myhost/script.cgi?parameter`” where “`http://myhost/script.cgi`” is the URL of the web script and “`parameter`” is an optional parameter that is passed to the script. A *URL parameter* can be retrieved inside a script by the I/O action

```
getUrlParameter :: IO String
```

which returns the part of the URL following the character “?”. Note that a URL parameter should be “URL encoded” to avoid the appearance of characters with a special meaning. The library `HTML.Base` provides the functions `urlencoded2string` and `string2urlencoded` to decode and encode such parameters, respectively.

As a simple example, we want to write a web script to navigate through a directory structure. The current directory is the URL parameter for this script. The script extracts this parameter by the use of `getUrlParameter` and shows all entries as a HTML list [\[Browse](#)

[Program](#)][[Download Program](#)] (the prelude function `mapM` applies a mapping from elements into actions to all elements of a list and collect all results in a list):

```
showDirPage :: IO HtmlPage
showDirPage = do
  param <- getUrlParameter
  let dir = if null param then "." else urlencoded2string param
      entries <- getDirectoryContents dir
      hexps <- mapM (entry2html dir) entries
  return $ page "Browse Directory"
           [h1 [htxt $ "Directory: " ++ dir], ulist hexps]
```

The I/O action `getDirectoryContents` is defined in the library `System.Directory` (in package `directory`) and returns the list of all entries in a directory. The function `entry2html` checks for an entry whether it is a directory. If this is the case, it returns a link to the same web script but with an extended parameter, otherwise it simply returns the entry name as an HTML text (`doesDirectoryExist` is defined in the library `System.Directory` and returns `True` if the argument is the name of a directory):

```
entry2html :: String -> String -> IO [HtmlExp]
entry2html dir e = do
  direx <- doesDirectoryExist (dir ++ "/" ++ e)
  if direx
    then return [href ("?" ++ string2urlencoded (dir ++ "/" ++ e))
                 [htxt e]]
    else return [htxt e]
```

## 7.9.2 Cookies

Cookies are small pieces of information (represented by strings) that are stored on the client's machine when a client communicates to a web server via his browser. The web server can send cookies to the client together with a requested web document. If the client wants to retrieve the same or another document from the web server, the client's browser sends the stored cookies together with the request for a document to the browser. Thus, cookies can be used to identify the client during a longer interaction with the web server (also across various web scripts stored on the same web browser). Hence, cookies are used to implement session data as described in Section 7.6. In this section, we describe more details about cookies if one is interested to implement his own session handling.

Basically, a cookie has a name and a value. Both parameters are of type `string`. Cookies can also have additional parameters to control their lifetime, validity for different web servers or regions on a web server etc (see definition of datatype `CookieParam` in the library `HTML.Base`) which we will not describe here. As the default, a cookie is a valid during the client's browser session for all documents in the same directory or a subdirectory in which the cookie was set.

The library `HTML.Base` provides two functions to set and retrieve cookies. As described above, a cookie is set by adding it with some web page. For doing so, there is the function

```
addCookies :: [(String,String)] -> HtmlPage -> HtmlPage
```

which adds a list of cookies, i.e., name/value pairs, to a web page. These cookies are submitted with the page to the client's browser. To retrieve cookies (that are previously sent), there is an I/O action

```
getCookies :: IO [(String,String)]
```

that returns the list of all cookies (i.e., name/value pairs) sent from the browser for the current HTML page.

As a simple example, we want to use cookies to write a web application where a user must identify himself and this identification is used in another independent script. The identification is done by setting a cookie of the form ("LOGINNAME", <name>) where <name> is the user's name. We implement a "login form" that sets this cookie as follows [\[Browse Program\]](#)[\[Download Program\]](#):

```
loginForm :: HtmlFormDef ()
loginForm = simpleFormDef
  [htxt "Enter your name: ", textField tref "",
    hrule,
    button "Login" handler
  ]
where
  tref free

  handler env = return $
    addCookies [("LOGINNAME", env tref)] $
      page "Logged In"
        [h2 [htxt $ env tref ++ ": thank you for visiting us"]]

-- A web page containing the login form:
loginPage :: IO HtmlPage
loginPage = return $ page "Login" [formElem loginForm]
```

First, the form asks the user for his name. The cookie is set together with the acknowledgment page (defined in function "handler").

Now we can write another web script that uses this cookie. This script shows the user's name or the string "Not yet logged in" if the user has not used the login form to set the cookie. Using the function `getCookies`, the implementation is quite simple (the function `lookup`, defined in the prelude, searches for a name in a name/value list; it returns "Nothing" if the name was not found and "Just v" if the first occurrence of the name in the list has the associated value v; the prelude function `maybe` processes these two cases) [\[Browse Program\]](#)[\[Download Program\]](#):

```
getNamePage :: IO HtmlPage
getNamePage = do
  cookies <- getCookies
  return $ page "Hello" $
    maybe [h1 [htxt "Not yet logged in"]]
```

```
(\n -> [h1 [htxt $ "Hello, " ++ n]])
(lookup "LOGINNAME" cookies)
```

As mentioned above, cookies need special support on the client’s side, i.e., the web browser of the client must support cookies. If cookies are essential for an application, one should check whether the client allows the setting of cookies. This can be done by trying to set a cookie and by checking whether this was successful. For instance, one can modify the above login script as follows. The first page immediately sets a cookie with name “SETCOOKIE”. Then the handler checks whether this cookie has been sent by the client’s browser. If this cookie is not received, it returns a page with the message “Sorry, can’t set cookies.” instead of the acknowledgment page which sets the cookie “LOGINNAME” [\[Browse Program\]](#)[\[Download Program\]](#):

```
loginPage :: IO HtmlPage
loginPage = return $
  addCookies [("SETCOOKIE","")] $ page "Login" [formElem loginForm]

loginForm :: HtmlFormDef ()
loginForm = simpleFormDef
  [htxt "Enter your name: ", textField tref "",
    hrule,
    button "Login" handler
  ]
where
  tref free

  handler env = do
    cookies <- get_cookies
    return $
      maybe (page "No cookies" [h2 [htxt "Sorry, can't set cookies."]])
        (\_ -> addCookies [("LOGINNAME",env tref)] $ page "Logged In"
          [h2 [htxt $ env tref ++ ": thank you for visiting us"]])
        (lookup "SETCOOKIE" cookies)
```

### 7.9.3 Style Sheets

The library `HTML.Base` provides various operations to add style sheets to web pages (`pageCSS`) or to add style classes to individual elements (e.g., `style`, `textstyle`, `blockstyle`). The package `html2` also contains libraries to use [Bootstrap](#) renderings in web pages, see library [HTML.Styles.Bootstrap4](#) for more details.

## Chapter 8

# Further Libraries for Application Programming

- Databases [\[17\]](#)
- Constraints
- GUI [\[15\]](#)
- XML
- Distributed Programming, ports [\[14\]](#)
- Metaprogramming

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